

JAYPEE UNIVERSITY OF INFORMATION TECHNOLOGY, WAKNAGHAT

TEST -2 EXAMINATION- 2023

B.Tech-I Semester (CSE/IT/ECE/CE/BT/BI)

COURSE CODE (CREDITS):22B1 WPH731

MAX. MARKS: 25

COURSE NAME: Computational Nanotechnology

COURSE INSTRUCTORS: Dr. Santu Baidya

MAX. TIME: 1 Hour 30 Minutes

---

*Note: (a) All questions are compulsory.*

*(b) Marks are indicated against each question in square brackets.*

*(c) The candidate is allowed to make suitable numeric assumptions wherever required for solving problems*

---

Q1) Write down the Hamiltonian for a material with  $N_e$  number of electrons and  $N_i$  number of ions and explain each term in the Hamiltonian. Write the eigenvalue equation (Schrodinger equation) for this Hamiltonian. [CO-3] [2+1]

Q2) What is Born-Oppenheimer approximation (explain from Hamiltonian)? Why is it called adiabatic approximation? [CO-3] [2+1]

Q3) Write down the Hartree approximation and explain how does it help to solve many-electron problem in materials? What is the disadvantage of the Hartree approximation to explain quantum state of electrons in a material. [CO-5] [2+1]

Q4) Write down the Slater determinant form of wave function for a 2-electron system (e.g., He). Show that a Slater determinant wave function represents correctly electronic wave function properties, such as Pauli exclusion principle and anti-symmetric property. [CO-3] [1+2]

Q5) What is exchange energy in Hartree-Fock approximation? Write the koopman's theorem from Hartree-Fock approximation. [CO-3] [1+2]

Q6) Write down the second order differential equation (Schrodinger equation) for an electron in a one dimensional infinite quantum potential well where potential function is defined as  $V(x) = 0$  for  $0 \leq x \leq a$  ( $a$  is the potential well width along  $x$  axis) and  $V(x) = \infty$  for  $x \geq a$  and  $x \leq 0$ . What is the eigenvalue for the  $n^{\text{th}}$  quantum state for this electron. Then write down the python code to solve the second order differential equation for the solution to this quantum mechanical problem. [CO-2] [2+3+5]