

Note: All questions are compulsory. Marks are indicated against each question in square brackets.

1. [2.5 + 2.5 = 5 Marks] [CO3]

- Explain what inverse properties are in ontology with the help of an example. For a particular property that exists in the ontology, add the correct inverse property axioms. You are not supposed to add new properties, only state that a property is the inverse of an other property if they already exist in the ontology.
- Can the graph shown in Figure A be decomposed into edge-disjoint spanning trees?

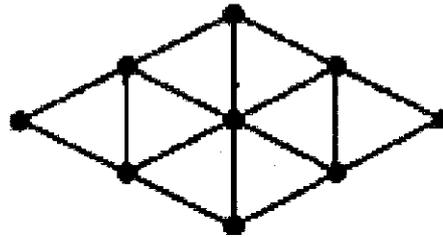


Figure A

2. [2.5 + 2.5 = 5 Marks] [CO4]

- Ordinarily, focused crawlers take as input traditional inputs such as some starting (or seed) URLs and, possibly, a topic description (e.g. a list of keywords). Think of at least two other novel input types. What domains would they particularly useful for?
- Draw the graph representation of the cipher snippet shown in Figure B.

```
CREATE (bob:Person {name: "Bob"})
CREATE (james:Person {name: "James"})
CREATE (stephen:Person {name: "Stephen"})
CREATE (sarah:Person {name: "Sarah"})
CREATE (google:Company {name: "Google"})
CREATE (tech:Sector {name: "Technology"})
CREATE (bob)-[:WORKSIN]->(tech)-[:COMPANY]->(google)
CREATE (stephen)-[:EMPLOYEDBY]->(google)
CREATE (james)-[:FRIEND]->(stephen)-[:SIBLING]->(sarah)
```

Figure B

3. [2.5 + 2.5 = 5 Marks] [CO3]

- Discuss the major steps involved in modeling an ontology.
- Discuss the major steps of an overall process model to build a knowledge graph.

4. [2.5 + 2.5 = 5 Marks] [CO2]

Prove or disprove:

- Every subgraph of a planar graph is planar.
- Every subgraph of a nonplanar graph is nonplanar.

5. [2.5 + 2.5 = 3 Marks] [CO2]

- For the graph G shown in Figure C, compute $\chi'(G)$ (edge chromatic number) and draw $L(G)$ (Line Graph).
- Prove that the chromatic number of a graph equals the maximum of the chromatic numbers of its components.

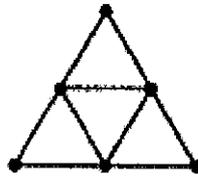


Figure C

6. [5 Marks] [CO2]

Figure D shows a flow network. The first value of each edge represents the flow, which is initially 0, and the second value represents the capacity. The value of the flow of a network is the sum of all the flows that get produced in the source s or equivalently to the sum of all the flows that are consumed by the sink t . A maximal flow is a flow with the maximal possible value. Find the maximal flow of a flow network.

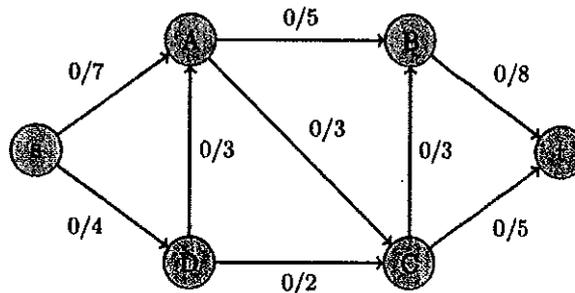


Figure D

7. [2.5 + 2.5 = 5 Marks] [CO1]

- Consider the CLIQUE problem restricted to graphs in which every vertex has degree at most 3. Call this problem CLIQUE-3. Prove that CLIQUE-3 is in NP.
- Proving NP-completeness by generalization. For the LONGEST PATH problem given below, prove that it is NPcomplete by showing that it is a *generalization* of some NP-complete problem. LONGEST PATH: Given a graph G and an integer g , and in G a simple path of length g .