

## JAYPEE UNIVERSITY OF INFORMATION TECHNOLOGY, WAKNAGHAT

(Summer Semester-Mid Term) - June-2018

COURSE CODE: 11B11MA201

MAX. MARKS: 50

COURSE NAME: Mathematics II

COURSE CREDITS: 04

MAX. TIME: 2 Hrs

*Note: All questions are compulsory. Carrying of mobile phone during examinations will be treated as case of unfair means.*

Q1. Discuss the convergence of  $\frac{x}{1+x} + \frac{x^2}{1+x^2} + \frac{x^3}{1+x^3} + \dots$  [8]

Q2. Find the power series solution of  $4xy'' + 2y' + y = 0$  about  $x=0$  [12]

Q3. Express  $J_{5/2}$  and  $J_{-5/2}$  in terms of sine and cosine. [8]

Q4. For Legendre polynomial  $P_n(x)$

show that  $nP_n(x) = (2n-1)xP_{n-1}(x) - (n-1)P_{n-2}(x)$  [8]

Q5. Express  $x^3 + 2x^2 + x - 3$  in terms of Legendre polynomial. [4]

Q6. For Chebyshev polynomial  $T_n(x)$  show that  $T_{n+1}(x) - 2xT_n(x) + T_{n-1}(x) = 0$  [5]

Q7. Express  $5x^3 + 3x + 2$  in terms of Chebyshev polynomial. [5]