## JAYPEE UNIVERSITY OF INFORMATION TECHNOLOGY, WAKNAGHAT TEST 3- 2025

## Ph.D.-I Semester (Mathematics)

COURSE CODE (CREDITS): 18P1WGE101 (3)

MAX, MARKS: 25

COURSE NAME: RESEARCH METHODOLOGIES (Department-specific)

COURSE INSTRUCTOR: P K PANDEY

MAX. TIME: 2 Hours

Note: (a) All questions are compulsory.

(b) The candidate is allowed to make suitable numeric assumptions wherever required for solving problems.

Q.No.	Question	Marks
Q1	Write the <i>Frenet-Serret</i> formula, and for the helix: $\vec{r}(s) = \langle 2\cos\frac{s}{\sqrt{13}}, 2\sin\frac{s}{\sqrt{13}}, \frac{3s}{\sqrt{13}} \rangle$ Compute the <i>Frenet frame T</i> , <i>N</i> , <i>B</i> , $\kappa$ , $\tau$ .	4
Q2	Compute the curvature and torsion of the curve: $\vec{r}(t) = \langle e^t \cos t, e^t \sin t, e^t \rangle, t \in \mathbb{R}; \text{ at } t = 0.$	4
Q3	Compute the curvature and torsion of the curve: $\vec{r}(t) = \langle \cos^2 t, \sin t \cos t, \sin t \rangle, t \in \mathbb{R}; \text{ at } t = \frac{\pi}{4}.$	4
Q4	Consider a surface, given by: $\vec{r}(u,v) = \langle u\cos v, u\sin v, u^2 + v \rangle$ ; $(u,v) \in \mathbb{R}^2$ Show that the above surface is smooth about $(u,v) = (1,0)$ . Find the unit normal and tangent plane to the given surface at $(u,v) = (1,0)$ .	4
Q5	Consider a solar collector surface, given by: $ \ddot{r}(u,v) = \langle u\cos v, u\sin v, u^2 \rangle; \ 0 \le u \le 1, 0 \le v \le 2\pi. $ Compute the surface area of the above surface patch.	4
Q6	Define the first fundamental form. Compute the first fundamental of a sphere of radius R. Also, give some applications of the first fundamental form.	5