

JAYPEE UNIVERSITY OF INFORMATION TECHNOLOGY, WAKNAGHAT

TEST 1 EXAMINATION - September 2017

B.Tech V Semester

COURSE CODE: 11B11EC513

MAX. MARKS: 15

COURSE NAME: Electromagnetic Engineering

COURSE CREDITS: 3

MAX. TIME: 1HR

Note: All questions are compulsory. Carrying of mobile phone during examinations will be treated as case of unfair means. Assume any missing data. Marks are indicated in parenthesis.

1. Let $\mathbf{D} = 20\rho^2\mathbf{a}_\rho + \cos\varphi\mathbf{a}_\varphi + z\mathbf{a}_z$ C/m². Use both sides of the Gauss's divergence theorem to find the total amount of charge lying within the closed surface bounded by $0 < \rho < 1$, $0 < \varphi < \pi$ and $0 < z < 2$. (5m)
2. An infinite line charge density of 10 nC/m lies along the x-axis in the free space. What is the electric field intensity at the point $P(1,2,3)$. Use the formula directly. (2m)
3. A point charge is at the point $(0, -10, 0)$, a line charge density of 20 nC/m exists along the y-axis from $-1 < y < 1$ and a surface charge density exists for $-1 < x < 1$ and $-1 < y < 1$ on $z = 0$ plane. Write the expression (do not solve the expression) for electric field intensity at the point $(10, 0, 0)$. (3m)
4. If $\mathbf{E} = \frac{2r}{(r^2+a^2)^2}\mathbf{a}_r$ V/m (a is a constant), find the amount of work done in moving the point charge of 25 nC from $P(r = 10, \theta = \frac{\pi}{2}, \varphi = \frac{\pi}{2})$ to $Q(r = 5, \theta = \frac{\pi}{4}, \varphi = \frac{\pi}{4})$. Show the path that you have considered. (3m)
5. The current density in a certain region is given by $\mathbf{J} = \frac{0.1}{r}e^{-10^6t}\mathbf{a}_r$ A/m². At $t = 1\mu\text{s}$, how much of the current is crossing the spherical surface $r = 5$. (2m)