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JAYPEE UNIVERSITY OF INFORMATION TECHNOLOGY, WAKNAGHAT TEST -1 EXAMINATIONS-2022

B.Tech-IV Semester (ECE)

COURSE CODE: 18B11MA413

MAX. MARKS: 15

COURSE NAME: DISCRETE MATHEMATICS

COURSE CREDITS: 3

MAX. TIME: 1 Hour

Note: All questions are compulsory. Carrying of mobile phone during examinations will be treated as case of unfair means. Marks are indicated against each question in square brackets.

Q1. Define the duality principle for sets. Write the dual statement for the following

$$(A \cap B) \cup (B \cap A^c) \cup (A \cap B^c) = U$$

Here superscript c denotes the complement, and U is the universal set.

[3]

Q2. Consider $A = \{2,3,4,5\}$, and $B = \{0,1,2,3\}$. Compute $A \times B$ and $B \times A$. Is $|A \times B| = |B \times A|$?

Q3. For the set $S = \{a, b, c, d, e, f, g, h\}$ which of the following are partitions (explain):

(i)
$$A_1 = \{a, b, c, d\}, A_2 = \{d, e, f, g, h\}.$$

(ii)
$$A_1 = \{a, b, c, d\}, A_2 = \{e, f, g\}, A_3 = \{h\}.$$
 [3]

Q4. Let R is a relation on a set $A = \{a, b, c, d\}$, given by $R = \{(a, a), (b, b), (a, c), (c, d)\}$. Then prove or disprove that R is:

- (i) Reflexive
- (ii) Irreflexive
- (iii) Transitive

[3]

Q5: Define directed graph of a relation? Represent the relation

 $R = \{(1,1), (2,1), (2,3), (1,3), (3,3), (3,4), (4,4)\}$ on set $A = \{1,2,3,4\}$ using a directed graph.