

JAYPEE UNIVERSITY OF INFORMATION TECHNOLOGY, WAKNAGHAT

TEST -2 EXAMINATION- 2016

M.Tech (ECE) 2nd Semester

COURSE CODE: 10M11EC211

MAX. MARKS: 25

COURSE NAME: Advanced Digital Signal Processing

COURSE CREDITS: 03

MAX. TIME: 1.5 HR

Note: All questions are compulsory.

Carrying of mobile phone during examinations will be treated as case of unfair means.

Write your assumptions clearly, if it is required.

1. Consider a narrowband spatially propagating signal with a speed of propagation c . The signal impinges on an $M = 2$ element ULA from an angle $\phi = 0^\circ$ with spacing d between the elements. For illustration purposes, let the temporal content of the signal be a pulse. [5 marks]
 - a. Let the time of arrival of the pulse at the first sensor be $t = 0$. At what time does the signal arrive at the second sensor?
 - b. Do any other angles ϕ produce the same delay between the sensors? Why?
 - c. Suppose now that we only have single sensor. Can we determine the angle from which a signal impinges on this sensor?

2. An ARMA process has an autocorrelation $\{\gamma_{xx}(m)\}$ whose z-transform is given as

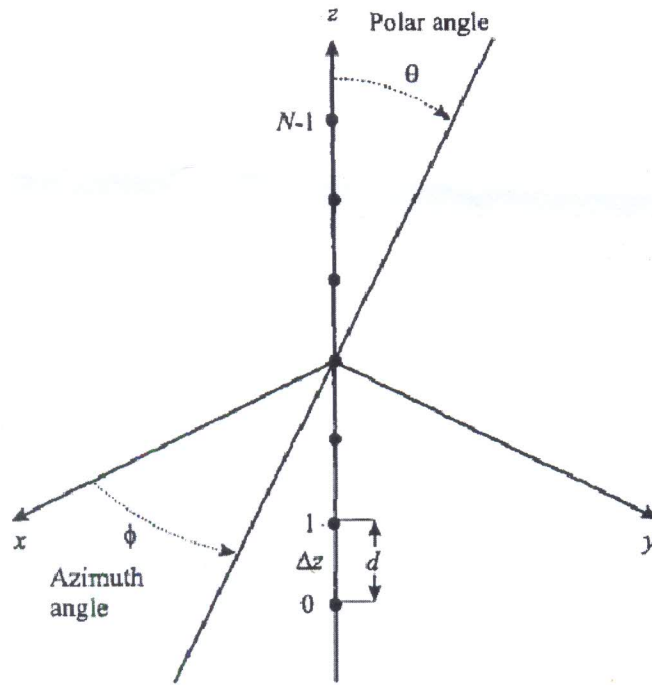
$$\Gamma_{xx}(z) = 9 \frac{\left(z - \frac{1}{3}\right)(z - 3)}{\left(z - \frac{1}{2}\right)(z - 2)}, \quad \frac{1}{2} < |z| < 2$$

- a. Determine the filter $H(z)$ for generating $\{x(n)\}$ from a white noise input sequence. Is $H(z)$ unique? Explain.
- b. Determine a stable linear whitening filter for the sequence $\{x(n)\}$. [6 marks]

3. Fill in the blank spaces [3 Marks]

- a. The spatial part of the processor is an aperture (or antenna) for the continuous space domain and an _____ for the discrete space domain.
- b. The array configuration consists of two parts. The first part is the _____ of the individual elements and the second part is the _____.

4. Assume a uniform linear array given below where N is even.



Use the relationships

$$B_{\psi}(\Psi) = 2\text{Re}[\mathbf{w}_1^H \mathbf{v}_{\psi_1}(\Psi)]$$

to derive the beam pattern of a uniformly weighted uniform linear array i.e.

$$B_{\psi}(\Psi) = \frac{1}{N} \left[\frac{\sin\left(\frac{N}{2}\Psi\right)}{\sin\left(\frac{\Psi}{2}\right)} \right] \quad -\frac{2\pi d}{\lambda} \leq \Psi \leq \frac{2\pi d}{\lambda}$$

Where \mathbf{v}_{ψ} is the array manifold vector, \mathbf{w}_1 contains the first half elements of weighing vector \mathbf{w} and $\Psi = \frac{2\pi}{\lambda} \cos(\theta) d$. [6 marks]

5. Let τ_{ij} is the time delay of arrival between the i^{th} and j^{th} element for a planar wave propagating along the unit vector \mathbf{a} . Assume \mathbf{r}_i and \mathbf{r}_j are the position vectors of the i^{th} and j^{th} element respectively, and c is the speed of propagation of the wave. Derive and express the τ_{ij} in terms of the position vectors of the elements. [5 Marks]