

## JAYPEE UNIVERSITY OF INFORMATION TECHNOLOGY, WAKNAGHAT

## TEST -1 EXAMINATION-2016

## B.Tech II Semester (CE)

COURSE CODE: 10B11MA201

MAX. MARKS: 15

COURSE NAME: Mathematics-II

COURSE CREDITS: 04

MAX. TIME: 1 HR

*Note: All questions are compulsory. Carrying of mobile phone during examinations will be treated as case of unfair means.*

1. Find the interval of convergence of the series  $\frac{x}{2!} + \frac{x^2}{4!} + \frac{x^3}{6!} + \dots + \frac{x^n}{(2n)!} + \dots$  [2.5]
2. Investigate the convergence of the series  $\sum_{n=1}^{\infty} \frac{1}{n(n+1)}$ . [2.5]
3. Determine a power series solution of the differential equation  $y'' + y = 0$  of the form  $\sum_{n=0}^{\infty} c_n x^n$ . [4]
4. Show that  $J_n(x) = x^n \sum_{m=0}^{\infty} \frac{(-1)^m x^{2m}}{2^{2m+n} m! (n+m)!}$ ,  $n \geq 0$  an integer, is a solution of the Bessel's equation  $x^2 y'' + xy' + (x^2 - n^2)y = 0$ . [6]