

COURSE CODE: 10B11EC301

MAX. MARKS: 50

COURSE NAME: SIGNALS AND SYSTEMS

COURSE CREDITS: 04

MAX. TIME: 2 HRS

*Note: All questions are compulsory. Carrying of mobile phone during examinations will be treated as case of unfair means.*

- Q1. (a) State and prove the convolution in time domain property of continuous-time Fourier transform (CTFT). [5]  
(b) State and prove the differentiation in frequency domain property of discrete-time Fourier transform (DTFT). [5]
- Q2. Consider the Fourier transform pair  $e^{-|t|} \leftrightarrow \frac{2}{1+\omega^2}$ . Determine the Fourier transform of  
(a)  $x(t) = te^{-|t|}$ , (b)  $x(t) = \frac{4t}{(1+t^2)^2}$  [5+5]
- Q3. Determine the Laplace transform, the associated ROC and pole-zero plot for each of the following signals:  
(a)  $x(t) = e^{-4t}u(t) + e^{-5t}(\sin 5t)u(t)$   
(b)  $x(t) = te^{-|t|}$  [5+5]
- Q4. (a) Explain various properties of ROC of z-transform. [5]  
(b) Let  $y[n] = \left(\frac{1}{9}\right)^n u(n)$ . Determine two distinct signals such that each signal has a z-transform  $X(z)$  which satisfies both of the following conditions:  
(i)  $\frac{X(z)+X(-z)}{2} = Y(z^2)$   
(ii)  $X(z)$  has only one pole and only one zero in the z-plane. [5]
- Q5. (a) Prove the sampling theorem. [5]  
(b) Describe the following:  
(i) Nyquist rate, under-sampling and over-sampling  
(ii) Types of practical sampling [3+2]