

JAYPEE UNIVERSITY OF INFORMATION TECHNOLOGY, WAKNAGHAT

Test -1 (September, 2015)

Department of Electronics and Communications Engineering

M.Tech. (First Semester)

Course Code: 13M1WEC132

Duration: 1 hour

Course Name: Mathematical Techniques for Engineering

Maximum Marks: 15

Note: Answer all questions. Each question carries three marks.

1. Perform the Gram-Schmidt orthogonalization on the basis $\{u_1, u_2, u_3\} = \{1, x, x^2\}$.
2. Find the first four terms in each portion of the series solution around $x_0 = -2$ for the differential equation $y'' - xy = 0$.
3. Solve the system $\frac{dy}{dx} + 2y = 1.3e^{-x}, y(0) = 5$ using the Euler's method. Compare the solution with the exact solution.
4. Solve $\frac{\partial u}{\partial x} + \frac{\partial u}{\partial t} + u = 0, x > 0, t > 0$ with $u(0, t) = 0, t > 0$ and $u(x, 0) = \sin(x), x > 0$ using the Laplace transforms.
5. Solve the equation $\int_0^\infty f(t) \cos \omega t = \begin{cases} 1 - \omega, & 0 \leq \omega \leq 1 \\ 0, & \omega > 1 \end{cases}$.