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JAYPEE UNIVERSITY OF INFORMATION TECHNOLOGY, WAKNAGHAT **TEST -3 EXAMINATION-2021**

B.Tech 7th Semester

COURSE CODE: 19B1WCI737

MAX. MARKS: 35

COURSE NAME: OPTIMIZATION METHODS IN BUSINESS ANALYTICS

COURSE CREDITS: 3

MAX. TIME:

Note: All questions are compulsory. Carrying of mobile phone during examinations will treated as case of unfair means.

1. Choose the correct option

[1+1+1+1+1]

A. Which of the following statement is false with respect to performing sensitivity analysis

a) Change in Constraint coefficient of basic variablesb) Change in Objective function coefficients of non basic variable

c) Change in Objective function coefficients of basic variable

d) Add a new constraint

B. Which of the following is/are invalid pair (change, remedy) for sensitivity analysis context

a) (Change in Objective function coefficients of non basic variable, Simplex)

b) (Change in Objective function coefficients of basic variable, Simplex)

c) (Change in RHS of constraint, simplex)

d) (Add a new constraint, Dual simplex)

C. Which is/are not a salient feature of transportation problem

a) Optimality of MODI or UV method

b) Economic Interpretation of Dual

c) balanced problems

d) integer solution

D. Which of the following is/are valid termination condition of non gradient optimization procedure, assume f is an objective function.

a) $\|\nabla f_{x=x_i}\|_2 \le \text{threshold}$

b) $|\nabla f_{x=x_i}| < \text{threshold}$

c) $|x_{i+1} - x_i| < \text{threshold}$

 \mathbf{d}) $\|\mathbf{x}_{i+1} - \mathbf{x}_i\|_2$ <threshold

E. Which one of the Hassian matrix does not satisfy convexity

$$a)\begin{bmatrix} 5 & 0 \\ 0 & 2 \end{bmatrix}$$

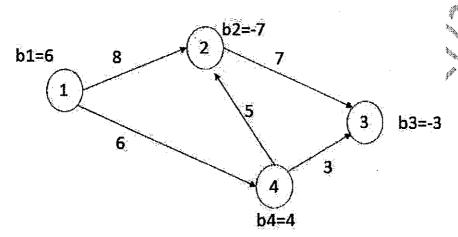
b)
$$\begin{bmatrix} -5 & 0 \\ 0 & 2 \end{bmatrix}$$

c)
$$\begin{bmatrix} 5 & 1 \\ 0 & 2 \end{bmatrix}$$

d)
$$\begin{bmatrix} -5 & 0 \\ 1 & 2 \end{bmatrix}$$

3. Explain Min cut theorem for max flow problem with duality. You may consider any arbitrary graph. [5]

4. Solve min cost flow of below graph? Consider b1,b2,b3 and b4 are respective resource at different nodes and edge weight represents the cost per unit for transporting the resource [5]



5. Find out the optimal solutions to minimize f(x,y) = 3x + y Such that, $x^2 + y^2 = 8$ and xy = 8. [5]

6. Explain the principal behind the expansion and contraction behind the simplex method. Please provide respective formula.

7. Find out the derivation of hessian matrix of objective function $f(x_1,x_2)$ with the constraints g_1 ,

g2, g3,g4 as given below. Please consider a minimization problem.



8. Solve the TSP with branch and bound methods for below distance data among the cities. Each cell(i,j) represents respective distance between i city to j city. Here we have 4 cities. [5]

$$\begin{bmatrix} - & 20 & 30 & 10 \\ 15 & - & 16 & 4 \\ 3 & 5 & - & 2 \\ 19 & 6 & 18 & - \end{bmatrix}$$