

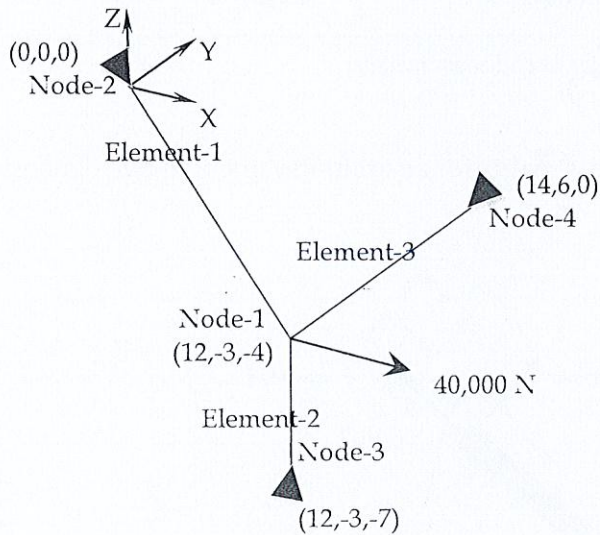
Course Code: 13M1WCE131  
Course Name: Finite Element Methods  
Course Credit: 03

Max. Marks: 35

Max. Time: 120 Minutes

Note: All questions are compulsory. Carrying of mobile phone during examination will be treated as case of unfair means. Assume any missing data.

Q.1 Analyse the space truss shown in Figure 1. The truss is composed of four nodes, whose coordinates (in meters) are shown in figure, and three elements, whose cross-sectional areas are all  $0.0002 \text{ m}^2$ . The modulus of Elasticity  $E=200 \text{ GPa}$  for all the elements. A load of  $40,000 \text{ N}$  is applied at node 1 in the global x-direction. Node 2-4 are pin supported and thus constrained from movement in the x, y and Z directions.



[6]

Figure 1: Space truss assembly

Q.2 Compare displacement and axial stress obtained from the finite element solution and exact solution for a bar element. (Assume minimum two elements in a bar element). The schematic view of bar element is shown in Figure 2.

[7]

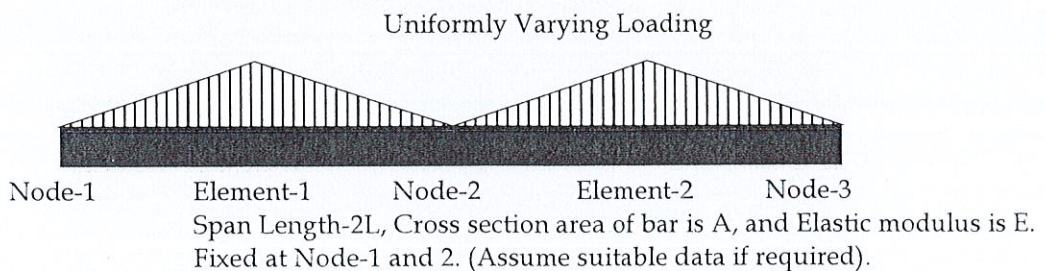


Figure 2: Bar member subjected to uniformly varying loading

Q.3. (a) Write the statement for the Euler-Bernouli Beam Theory with the engineering application.

(b) Develop a beam stiffness matrix including bending deformation only.

(c) Plot the shape function for the same (beam).

[2+3+3]

Q.4. Determine the displacement and rotation under the force and moment located at the centre of the beam shown in Figure 3. The beam has been discretised into the two elements, as shown in Figure. The beam is fixed at both ends. A downward force of 20 kN and an applied moment of 50 kN-m act at the centre of the beam. Elastic modulus  $E$  is 200 GPa and Moment of Inertia is  $0.0005 \text{ m}^4$  throughout the beam length. Also plot the nodal forces and moments, which are acting on each element. [8]

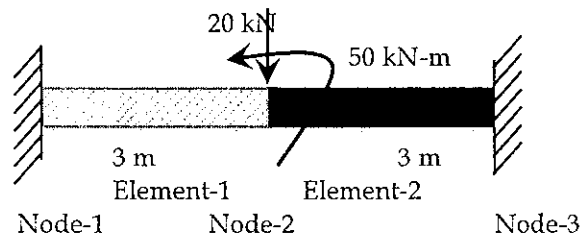


Figure 3: Fixed end beam member

Q.5 Develop a global elemental stiffness matrix for an arbitrarily oriented two dimensional beam element shown in Figure 4. [6]

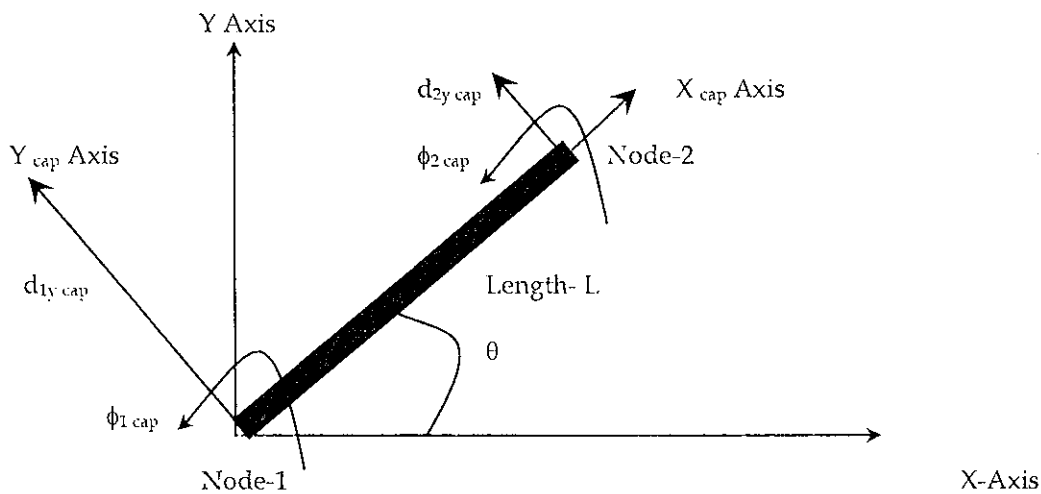


Figure 4: Arbitrarily oriented beam element