

## JAYPEE UNIVERSITY OF INFORMATION TECHNOLOGY, WAKNAGHAT

TEST-3 EXAMINATION- December, 2018

M. Tech III Semester

COURSE CODE: 15M1WCI331

MAX. MARKS: 35

COURSE NAME: Advanced Theory of Computation

COURSE CREDITS: 3

MAX. TIME: 120 Minutes

*Note: All questions are compulsory. Carrying of mobile phone during examinations will be treated as case of unfair means.*

- Q1. Definition of a language  $L$  with alphabet  $\{a\}$  is given as following.  $L = \{a^{nk} \mid k > 0, \text{ and } n \text{ is a positive integer constant}\}$  What is the minimum number of states needed in a DFA to recognize  $L$ ? (3) (CO1)
- Q2. Construct PushDown Automata for  $L = \{0^n 1^m 2^m 3^n\}$ . Trace the acceptance of the following string by this PDA : 00011112222333. (4) (CO2)
- Q3. Which of the following problems are decidable? Support your answer with appropriate explanation. (6) (CO5)
- 1) Does a given program ever produce an output?
  - 2) If  $L$  is a context-free language, then is  $L'$  (complement of  $L$ ) also context-free?
  - 3) If  $L$  is a regular language, then is  $L'$  also regular?
  - 4) If  $L$  is a recursive language, then, is  $L'$  also recursive?
- Q4. Does the PCP with two lists  $x = (b, bab^3, ba)$  and  $y = (b^3, ba, a)$  have a solution? (3) (CO5)
- Q5. Describe the class of languages accepted by different machines in Automata theory. Draw a Venn Diagram also for the same. (7) (CO6)
- Q6. Draw a TM for subtraction operation. eg. (3-4) or (4-3) (6) (CO6)
- Q7. What are NP, P, NP-complete and NP-Hard problems? (6) (CO7)