Dr. Mandeep Singh

JAYPEE UNIVERSITY OF INFORMATION TECHNOLOGY, WAKNAGHAT T-1, EXAMINATION- February-2020

B.Tech. II Semester (BI/BT)

COURSE CODE: 18B11MA212

MAX. MARKS: 15

COURSE NAME: BASIC MATHEMATICS-II

COURSE CREDITS: 04

MAX. TIME: 1:00 Hrs.

Note: All questions are compulsory. Carrying of mobile phone during examinations will be treated as case of unfair means.

Quest (1) Examine the convergence of the series

[CO-1][3]

$$\sum_{n=1}^{\infty} \frac{\sqrt{(n+1)} - 1}{(n+2)^3 - 1}$$

Quest (2) Test the following series for absolute convergence and conditional convergence.

$$\sum_{n=1}^{\infty} (-1)^{n+1} \frac{1+n}{n^2}.$$

[CO-1][3]

Quest (3) Express $\frac{\partial w}{\partial u}$ and $\frac{\partial w}{\partial v}$ in terms of u and v by using Chain rule if $w=xy+yz+zx, \quad x=u+v, \quad y=u-v, \quad z=uv$.

$$w = xy + yz + zx$$
, $x = u + v$, $y = u - v$, $z = uv$

[CO-2][3]

Quest (4) If $u = \tan^{-1} \left(\frac{x^3 + y^3}{\sqrt{x} + \sqrt{y}} \right)$, then find the value of

[CO-2][3]

$$x\frac{\partial u}{\partial x} + y\frac{\partial u}{\partial y}$$

Quest (5) Using Taylor's Theorem, expand $f(x,y) = e^{2x+y}$ about the point (0,0), upto second degree [CO-2][3]