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JAYPEE UNIVERSITY OF INFORMATION TECHNOLOGY, WAKNAGHAT

TEST - 1 EXAMINATION – FEBRUARY 2020

B.TECH IV SEMESTER (ECE)

COURSE CODE: 18B11EC412

MAX. MARKS: 15

COURSE NAME: FUNDAMENTALS OF SIGNALS AND SYSTEMS

COURSE CREDITS: 04

MAX. TIME: 1Hr.

Note: All questions are compulsory. Carrying of mobile phone during examinations will be treated as case of unfair means.

1(a). Sketch the following signals:

[CO-1]

1

- (i) u(t-5) u(t-7)
- (ii) $t^2[u(t-1) u(t-2)]$
- (b). Simplify the following expressions:

[CO-1]

1

- $(i)\left(\frac{sint}{t^2+2}\right)\delta(t)$
- (ii) $[e^{-t}\cos(3t 60^0)]\delta(t)$
- (c). Evaluate the following integrals

[CO-1]

1

- (i) $\int_{-1}^{1} (3t^2 + 1)\delta(t)dt$
- (ii) $\int_{-\infty}^{\infty} (t^2 + cos\pi t) \delta(t-1) dt$
- (d). Determine whether or not each of the following signals is periodic. If signal is periodic, determine it fundamental period.

[CO-1]

1

- (i) $x(t) = \sin^2 t$ (ii) $x(t) = \cos t + \cos t$
- (i) x(t) = sin²t
 (ii) x(t) = cost + sin√2 t
 (e) Determine whether the following are causal or non causal system

[CO-1]

1

- (i) $y(t) = x^2(t-1)$
- (ii) y(t) = x(t+5)
- 2(a). Determine convolution of a function f(t) with a unit impulse.

[CO-2]

1

(b). Explain how causality restrictions on both signals and systems

[CO-2]

2

simplify the limits of integration in equation

$$y(t) = f(t) * h(t) = \int_{-\infty}^{\infty} f(\tau)h(t - \tau)d\tau$$

- (c). Using direct integration, find $e^{-at}u(t)*e^{-bt}u(t)$ for $t\ge 0$ and t< 0 [CO-2] 2
- 3(a). Summarize the steps for graphical convolution. [CO-2] 1
- (b). Compute y(t) = u(t)*u(t) for t<0 and $t\ge0$. Show all graphical steps of [CO-2] 2 convolution.
- (c). Find y₀(t), the zero input component of the response for an LTI system [CO-2] 2 described by the following differential equation:

$$(D^2 + 5D + 6)y(t) = Df(t)$$

When the initial condition are $y_0(0) = 0$, $y_0(0) = -8$