"Seismic Analysis and Design of a four storey RC Building"

## A PROJECT

Submitted in partial fulfillment of the requirements for the award of the degree of BACHELOR OF TECHNOLOGY IN

CIVIL ENGINEERING
Under the supervision of Prof. Poonam Dhiman

By
Dilpuneet Singh (121614)

## to



JAYPEE UNIVERSITY OF INFORMATION TECHNOLOGY

WAKNAGHAT SOLAN - 173234

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## CERTIFICATE

This is to certify that the work which is being presented in the project title "Seismic Analysis and Design of RC building" in partial fulfilment of the requirements for the award of the degree of Bachelor of technology and submitted to Civil Engineering Department, Jaypee University of Information Technology, Waknaghat is an authentic record of work carried out by Dilpuneet Singh (121614) during a period from July 2015 to December 2015 under the supervision of Prof. Poonam Dhiman Assistant Professor, Civil Engineering Department, Jaypee University of Information Technology, Waknaghat.

The above statement made is correct to the best of my knowledge.

Date: -

Prof. Dr. Ashok Kumar Gupta
Professor \& Head of Department
Civil Engineering Department
JUIT Waknaghat

Mrs. Poonam Dhiman
Assistant Professor
Civil Engineering Department
JUIT Waknaghat

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## ABSTRACT

In this project first static and dynamic analysis of four storey reinforced concrete building was carried out. The calculations were carried out first manually for both the methods then same calculations were done using staad pro. The results of analysis in terms of member forces were compared and it was found that response spectrum dynamic analysis is more economical as compared to static. Design of beams and columns was carried out by preparing spread sheets for doubly reinforced beams and columns under biaxial bending. The seismic analysis and design is done which will ensure safe building during earthquake.

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# Chapter 1 Introduction 

## 1.Introduction

Earthquake-resistant structures are structures designed to withstand earthquakes. While no structure can be entirely immune to damage from earthquakes, the goal of earthquake-resistant construction is to erect structures that fare better during seismic activity than their conventional counterparts.
According to building codes, earthquake-resistant structures are intended to withstand the largest earthquake of a certain probability that is likely to occur at their location. This means the loss of life should be minimized by preventing collapse of the buildings for rare earthquakes while the loss of functionality should be limited for more frequent one.
Currently, there are several design philosophies in earthquake engineering, making use of experimental results, computer simulations and observations from past earthquakes to offer the required performance for the seismic threat at the site of interest. These range from appropriately sizing the structure to be strong and ductile enough to survive the shaking with an acceptable damage, to equipping it with base isolation or using structural vibration control technologies to minimize any forces and deformations. While the former is the method typically applied in most earthquake-resistant structures, important facilities, landmarks and cultural heritage buildings use the more advanced (and expensive) techniques of isolation or control to survive strong shaking with minimal damage. Examples of such applications are the Cathedral of Our Lady of the Angels and the Acropolis Museum.

In this project we will do seismic analysis of the four storey RC building with equivalent lateral force method and response spectrum method. In response spectrum we will first analysis without considering the infill wall and then with considering infill wall. We will calculate forces with both methods and then will compare the forces from the two methods. Our building is a plane frame model with four storeys.We will then do seismic analysis by staad pro and calculate results by both manually and staad pro. Then we will do design of beams and columns of the building.

# Chapter 2 <br> Methods of Seismic Analysis 

## 2. Methods of seismic analysis

Seismic analysis is a subset of structural analysis and is the calculation of the response of a building (or nonbuilding) structure to earthquakes. It is part of the process of structural design, earthquake engineering or structural assessment and retrofit in regions where earthquakes are prevalent.

### 2.1 Equivalent Static Lateral Force Method

The concept employed in equivalent static lateral force procedures is to place static loads on a structure with magnitudes and direction that closely approximate the effects of dynamic loading caused by earthquakes. Concentrated lateral forces due to dynamic loading tend to occur at floor and ceiling/roof levels in buildings, where concentration of mass is the highest. Furthermore, concentrated lateral forces tend to be larger at higher elevations in a structure. Thus, the greatest lateral displacements and the largest lateral forces often occur at the top level of a structure (particularly for tall buildings).

### 2.2 Response Spectrum Method

With the advent of personal computers and improved structural analysis techniques, the use of more precise methods increased. One of the most popular was response spectrum analysis. The method requires the determination of a response spectrum from measured seismic activity. This data was then reduced into a spectrum of seismic action versus natural frequency. The seismic action could be displacement, velocity, or acceleration, although the typical value used was acceleration. Detailed information from the structural model was coupled with the corresponding spectral values for each specific mode of vibration. The independent results were then combined using an appropriate technique to determine the response of the overall structure.

### 2.3 Time History Method

Time-History analysis is a step-by-step procedure where the loading and the response history are evaluated at successive time increments, $\Delta \mathrm{t}$ - steps. During each step the response is evaluated from the initial conditions existing at the beginning of the step (displacements and velocities) and the loading history in the interval. With this method the non-linear behaviour may be easily considered by changing the structural properties (e.g. stiffness, k) from one step to the next. Therefore this method is one of the most effective for the solution of non-linear response, among the many methods available. Nevertheless, in the present text, a linear time history analysis is adopted i.e. the structural properties are assumed to remain constant during the entire loading history and further it is assumed that the structure behaves linearly.

# Chapter 3 <br> Design <br> Example <br> Problem 

## 3. Design Example Problem

### 3.1 Introduction

A four storey RC building has been analysed by the equivalent static method, response spectrum method and time history method as per IS 1893 (Part 1): 2002. The example illustrates step by step procedure for determination of forces. One of the plane frame in transverse direction has been considered for the purpose of illustration by assuming that the building is symmetric in elevation and planned as shown in figure 3.1. The preliminary building data required for analysis are assumed in table 3.1.The building is evaluated by three methods i.e. Equivalent static lateral force method, response spectrum method and time history method.


Fig. 3.1 Plane frame structure model

Table 3.1 Assumed preliminary data required for analysis of frame

| 1. | Type of structure | Multi storey rigid joined plane frame |
| :--- | :--- | :--- |
| 2. | Seismic zone | V (table 2, IS 1893 (Part1): 2002) |
| 3. | Number of storeys | Four (G+3) |
| 4. | Floor height | 3.5 m |
| 5. | Infill wall | 300 mm thick including plaster in <br> longitudinal and 200 <br> direction in transverse |
| 6. | Imposed load | $3.5 \mathrm{kN} / \mathrm{m}^{2} \quad$Concrete (M 20) and Reinforcement <br> $(\mathrm{Fe} 415)$ |
| 7. | Materials | $300 \mathrm{~mm} \times 500 \mathrm{~mm} \quad$$300 \mathrm{~mm} \times 450 \mathrm{~mm}$ in longitudinal and <br> $300 \mathrm{~mm} \times 400 \mathrm{~mm}$ in transverse direction |
| 8. | Size of columns | 350 mm thick |
| 9. | Size of beam | $25 \mathrm{kN} / \mathrm{m}^{2}$ |
| 10. | Depth of slab | $20 \mathrm{kN} / \mathrm{m}^{2}$ |
| 11. | Specific weight of RCC | Rock |
| 12. | Specific weight of infill | As per IS 1893 (Part 1): 2002 |
| 13. | Type of soil | Compatible to IS 1893 (Part 1): 2002 <br> spectra at rocky site for 5\% damping |
| 14. | Response spectra | Time History |

### 3.2 Equivalent Static Lateral Force Method

A step by step procedure for analysis of the frame by equivalent static lateral force method is as follow:

### 3.2.1 Step1: Calculation of Lumped Masses to various floor levels

The earthquake forces shall be calculated for the full dead load plus the percentage of imposed load as given in Table 8 of IS 1893 (Part 1): 2002. The imposed load on roof is assumed to be zero. The lumped masses of each floor are worked out as follows:

## Roof

Mass of infill + Mass of columns + Mass of beams in longitudinal and transverse direction of that floor + Mass of slab + Imposed load of that floor if permissible.
$=\{((0.3 \times 10 \times(3.5 / 2)+0.2 \times 15 \times(3.5 / 2)) 20\}+\{(0.3 \times 10 \times 0.45+0.3 \times 15 \times 0.4) 25\}+\{0.15 \times 5 \times 10$
$\times 25\}+\{(0.3 \times 0.5 \times(3.5 / 2) \times 3) \times 25\}+0^{*}$
$=495.9375 \mathrm{kN}($ weight $)=50.57$ ton $($ mass $)$
$\mathbf{3}^{\text {rd }}, \mathbf{2}^{\text {nd }}, \mathbf{1}^{\text {st }}$ Floors
$=\{((0.3 \times 10 \times 3.5)+(0.2 \times 15 \times 3.5)) 20\}+\{(0.3 \times 10 \times 0.45+0.3 \times 15 \times 0.4) 25\}+\{0.15 \times 5 \times 10 \times$ $25\}+\{0.3 \times 0.5 \times 3.5 \times 3 \times 25\}+\left\{5 \times 10 \times 3.5 \times 0.5^{* *}\right\}$
$=813.125 \mathrm{kN}($ weight $)=82.91$ ton $($ mass $)$
*imposed load on roof not considered.
$* * 50 \%$ of imposed load, if imposed load is greater than $3 \mathrm{kN} / \mathrm{m}^{2}$.

## Seismic weight of building

$=$ Seismic weight of all floors $=\mathrm{M}_{1}+\mathrm{M}_{2}+\mathrm{M}_{3}+\mathrm{M}_{4}$
$=82.91+82.91+82.91+50.57=299.3$ ton

### 3.2.2 Step 2: Determination of Fundamental Natural Period

The approximate fundamental natural period of a vibration $\left(T_{a}\right)$, in seconds, of a moment resisting frame building without brick infill panels may be estimated by the empirical expression
$\mathrm{T}_{\mathrm{a}}=0.075 \times \mathrm{h}^{0.75}=0.075 \times 14^{0.75}=0.5423 \mathrm{sec}$
where h is the height of the building, in meters.

### 3.2.3 Step 3: Determination of Design Base Shear

Design seismic base shear, $V_{B}=A_{h} \times W$
$\mathrm{A}_{\mathrm{h}}=\left(\mathrm{Z} \times \mathrm{I} \times \mathrm{S}_{\mathrm{a}}\right) /(2 \times \mathrm{R} \times \mathrm{g})=(0.36 \times 1 \times 1.842) /(2 \times 5)=0.066312$
For $\mathrm{T}_{\mathrm{a}}=0.5423$
$\mathrm{S}_{\mathrm{a}} / \mathrm{g}=1 / \mathrm{T}_{\mathrm{a}}=1.842$, for rock site from figure 2 of IS 1893 (Part 1): 2002
Design seismic base shear, $\mathrm{V}_{\mathrm{B}}=0.066312 \times(299.3 \times 9.81)=194.7 \mathrm{kN}$

### 3.2.4 Step 4: Vertical Distribution of Base Shear

The design base shear $\left(\mathrm{V}_{\mathrm{B}}\right)$ computed shall be distributed along the height of the building as per the expression,
$\mathrm{Q}_{\mathrm{i}}=\mathrm{V}_{\mathrm{B}} \times \mathrm{W}_{\mathrm{i}} \times \mathrm{h}_{\mathrm{i}}{ }^{2} / \sum_{i=1}^{n} W_{i} \boldsymbol{h}_{i}{ }^{2}$
where,
$\mathrm{Q}_{\mathrm{i}}=$ Design lateral forces at floor i ,
$\mathrm{W}_{\mathrm{i}}=$ Seismic weights of the floor i ,
$h_{i}=$ Height of the floor $i$, measured from base, and
$\mathrm{n}=$ Number of stories

Using the equation 3.1, base shear is distributed as follows:
$\mathrm{Q}_{1}=\mathrm{V}_{\mathrm{B}}\left(\mathrm{W}_{1} \mathrm{~h}_{1}{ }^{2} / \mathrm{W}_{1} \mathrm{~h}_{1}{ }^{2}+\mathrm{W}_{2} \mathrm{~h}_{2}{ }^{2}+\mathrm{W}_{3} \mathrm{~h}_{3}{ }^{2}+\mathrm{W}_{4} \mathrm{~h}_{4}{ }^{2}\right)$
$=194.7\left(813.125 \times 3.5^{2} / 813.125 \times 3.5^{2}+813.125 \times 7^{2}+813.125 \times 10.5^{2}+495.9375 \times 14^{2}\right)$
$=8.19 \mathrm{kN}$

Similarly,
$\mathrm{Q}_{2}=0.1684 \times 194.7=32.78 \mathrm{kN}$
$\mathrm{Q}_{3}=0.3788 \times 194.7=73.75 \mathrm{kN}$
$\mathrm{Q}_{4}=0.4107 \times 194.7=79.96 \mathrm{kN}$


Fig. 3.2 Lateral force distribution at various floor level

### 3.3 Response Spectrum Method

## A:Frame without considering the stiffness of infills

A step by step procedure for analysis of the frame by response spectrum method is as follows:

### 3.3.1 Step 1: Determination of Eigenvalues and Eigenvectors

Mass matrix, M and stiffness matrix, K of the plane frame lumped mass model are,
$\mathrm{M}=\left[\begin{array}{cccc}M_{1} & 0 & 0 & 0 \\ 0 & M_{2} & 0 & 0 \\ 0 & 0 & M_{3} & 0 \\ 0 & 0 & 0 & M_{4}\end{array}\right]=\left[\begin{array}{cccc}82.91 & 0 & 0 & 0 \\ 0 & 82.91 & 0 & 0 \\ 0 & 0 & 82.91 & 0 \\ 0 & 0 & 0 & 50.57\end{array}\right]$ ton
Column stiffness of storey,
$\mathrm{k}=12 \mathrm{EI} / \mathrm{L}^{3}=\left(12 \times 22360 \times 10^{3} \times\left(0.3 \times 0.5^{3} / 12\right)\right) / 3.5^{3}=19556.85 \mathrm{kN} / \mathrm{m}$
Total lateral stiffness of each storey,
$\mathrm{k}_{1}=\mathrm{k}_{2}=\mathrm{k}_{3}=\mathrm{k}_{4}=3 \times 19556.85=58670.55 \mathrm{kN} / \mathrm{m}$
Stiffness of lumped mass modified structure
$\mathrm{K}=\left[\begin{array}{cccc}k_{1}+k_{2} & -k_{2} & 0 & 0 \\ -k_{2} & k_{2}+k_{3} & -k_{3} & 0 \\ 0 & -k_{3} & k_{3}+k_{4} & -k_{4} \\ 0 & 0 & -k_{4} & k_{4}\end{array}\right]$
$=\left[\begin{array}{cccc}117341.1 & -58670.55 & 0 & 0 \\ -58670.55 & 117341.1 & -58670.55 & 0 \\ 0 & -58670.55 & 117341.1 & -58670.55 \\ 0 & 0 & -58670.55 & 58670.55\end{array}\right] \mathrm{kN} / \mathrm{m}$

For the above stiffness and mass matrix, eigenvalues and eigenvectors are worked out as follows:
$\left|K-\omega^{2} m\right|=\left|\begin{array}{cccc}2 k-\omega^{2} m & -k_{2} & 0 & 0 \\ -k_{2} & 2 k-\omega^{2} m & -k 3 & 0 \\ 0 & -k_{3} & 2 k-\omega^{2} m & -k_{4} \\ 0 & 0 & -k_{4} & k-\omega^{2} m\end{array}\right|=0$
Taking $\mathrm{k} / \mathrm{m}=\omega_{\mathrm{n}}{ }^{2}$
Therefore,
$\left(\omega_{\mathrm{n}}{ }^{2}\right)^{4}-8.3\left(\omega_{\mathrm{n}}{ }^{2}\right)^{3}\left(\omega^{2}\right)+10.75\left(\omega_{\mathrm{n}}^{2}\right)^{2}\left(\omega^{2}\right)^{2}-4.45\left(\omega_{\mathrm{n}}^{2}\right)\left(\omega^{2}\right)^{3}+0.575\left(\omega^{2}\right)^{4}=0$
By solving the above equation, natural frequencies (eigenvalues) of various modes are

## Eigenvalues

$\left[\omega^{2}\right]=\left[\begin{array}{llll}81 & & & \\ & 657 & & \\ & & 1475 & \\ & & & 2065\end{array}\right]$
$\omega_{1}{ }^{2}=81, \omega_{2}{ }^{2}=657, \omega_{3}{ }^{2}=1475, \omega_{4}{ }^{2}=2065$
The quantity of $\omega_{\mathrm{i}}{ }^{2}$, is called the $\mathrm{i}^{\text {th }}$ eigenvalue of the matrix $\left\lfloor-M \omega_{i}{ }^{2}+K\right\rfloor \Phi_{i}$. Each natural frequency $\left(\omega_{\mathrm{i}}\right)$ of the system has a corresponding eigenvector (mode shape), which is denoted by $\Phi_{\mathrm{i}}$. The mode shape corresponding to each natural frequency is determined from the equations
$\left\lfloor-M \omega 1^{2}+K\right\rfloor \Phi_{1}=0$
$\left\lfloor-M \omega_{2}{ }^{2}+K\right\rfloor \Phi_{2}=0$
$\left\lfloor-M \omega 3^{2}+K\right\rfloor \Phi_{3}=0$
$\left\lfloor-M \omega 4^{2}+K\right\rfloor \Phi_{4}=0$

Solving the above equation, modal vector (eigenvectors), mode shapes and natural periods under different modes are

Eigenvectors $\{\Phi\}$
$\{\Phi\}=\left\{\Phi_{1} \Phi_{2} \Phi_{3} \Phi_{4}\right\}=\left[\begin{array}{cccc}-0.0328 & 0.0795 & 0.0808 & -0.0397 \\ -0.0608 & 0.0644 & -0.0540 & 0.0690 \\ -0.0798 & -0.0273 & -0.0448 & -0.0799 \\ -0.0872 & -0.0865 & 0.0839 & 0.0696\end{array}\right]$
Mode Shapes


Fig. 3.3 Modal Shapes

Natural time period
$\mathrm{T}=\left[\begin{array}{cccc}0.6977 & 0 & 0 & 0 \\ 0 & 0.2450 & 0 & 0 \\ 0 & 0 & 0.1636 & 0 \\ 0 & 0 & 0 & 0.1383\end{array}\right] \mathrm{s}$

### 3.3.2 Step 2: Determination of Modal Participation Factors

The modal participation factor $\left(\mathrm{p}_{\mathrm{k}}\right)$ of mode k is,
$\mathrm{p}_{\mathrm{k}}=\frac{\sum_{i=1}^{n} W_{i} \phi_{i k}}{\sum_{i=1}^{n} W_{i}\left(\phi_{i k}\right)^{2}}$
$\mathrm{p}_{1}=\frac{\sum_{i=1}^{4} W_{i} \phi_{i 1}}{\sum_{i=1}^{4} W_{i}\left(\phi_{i 1}\right)^{2}}=\frac{\left(W_{1} \phi_{11}+W_{2} \phi_{21}+W_{3} \phi_{31}+W_{4} \phi_{41}\right)}{\left(W_{1}\left(\phi_{11}\right)^{2}+W_{2}\left(\phi_{21}\right)^{2}+W_{3}\left(\phi_{31}\right)^{2}+W_{4}\left(\phi_{41}\right)^{2}\right)}=-14.45$
$\mathrm{p}_{2}=\frac{\sum_{i=1}^{4} W_{i} \phi_{i 2}}{\sum_{i=1}^{4} W_{i}\left(\phi_{i 2}\right)^{2}}=\frac{\left(W_{1} \phi_{12}+W_{2} \phi_{22}+W_{3} \phi_{32}+W_{4} \phi_{42}\right)}{\left(W_{1}\left(\phi_{12}\right)^{2}+W_{2}\left(\phi_{22}\right)^{2}+W_{3}\left(\phi_{32}\right)^{2}+W_{4}\left(\phi_{42}\right)^{2}\right)}=4.06$
Similarly,
$\mathrm{p}_{3}=2.1, \mathrm{p}_{4}=-0.52$

### 3.3.3 Step 3: Determination of Modal Mass

The modal mass $\left(\mathrm{M}_{\mathrm{k}}\right)$ of mode k is given by,
$\mathrm{M}_{\mathrm{k}}=\frac{\left[\sum_{i=1}^{n} W_{i} \phi_{i k}\right]^{2}}{g\left[\sum_{i=1}^{n} W_{i}\left(\phi_{i k}\right)^{2}\right]}$
where,
$\mathrm{g}=$ Acceleration due to gravity,
$\Phi_{\mathrm{ik}}=$ Mode shape coefficient at floor i in mode k , and
$\mathrm{W}_{\mathrm{i}}=$ Seismic weight of floor i ,
$\mathrm{M}_{1}=\frac{\left[\sum_{i=1}^{4} W_{i} \phi_{i 1}\right]^{2}}{g\left[\sum_{i=1}^{4} W_{i}\left(\phi_{i 1}\right)^{2}\right]}$
$\mathrm{M}_{1}$
$\frac{[9.81(82.91(-0.0328)+82.91(-0.0608)+82.91(-0.0798)+50.57(-0.0872))]^{2}}{9.81\left[9.81\left(82.91(-0.0328)^{2}+82.91(-0.0608)^{2}+82.91(-0.0798)^{2}+50.57(-0.0872)^{2}\right)\right]}$
$=269.85$
$\mathrm{M}_{2}=\frac{\left[\sum_{i=1}^{4} W_{i} \phi_{i 2}\right]^{2}}{g\left[\sum_{i=1}^{4} W_{i}\left(\phi_{i 2}\right)^{2}\right]}$, similarly, $\mathrm{M}_{2}=21.42, \mathrm{M}_{3}=5.78, \mathrm{M}_{4}=0.34$

Modal contributions of various modes
For mode $1, \frac{M_{1}}{M}=\frac{269.85}{299.3}=0.90=90 \%$

For mode 2, $\frac{M_{2}}{M}=\frac{21.42}{299.3}=0.0715=7.15 \%$
For mode 3, $\frac{M_{3}}{M}=\frac{5.78}{299.3}=0.0193=1.93 \%$
For mode $4, \frac{M_{4}}{M}=\frac{0.34}{299.3}=0.0011=0.11 \%$

### 3.3.4 Step 4: Determination of lateral force at each floor in each mode

The design lateral force ( $\mathrm{Q}_{\mathrm{ik}}$ ) at floor i in mode k is given by,
$\mathrm{Q}_{\mathrm{ik}}=\mathrm{A}_{\mathrm{k}} \Phi_{\mathrm{ik}} \mathrm{P}_{\mathrm{k}} \mathrm{W}_{\mathrm{i}}$
where,
$\mathrm{A}_{\mathrm{k}}=$ Design horizontal acceleration spectrum value as per clause 6.4.2 of IS 1893 (Part 1): 2002 using the natural period of vibration $\left(T_{k}\right)$ of mode $k$,

The design horizontal seismic coefficient $\mathrm{A}_{\mathrm{h}}$ for various modes are,
$\mathrm{A}_{\mathrm{hk}}=\frac{Z}{2} \frac{I}{R} \frac{S_{a k}}{g}$
$\mathrm{A}_{\mathrm{h} 1}=\frac{Z}{2} \frac{I}{R} \frac{S_{a 1}}{g}=\frac{0.36}{2} \frac{1}{5} 1.433=0.0515$
$\mathrm{A}_{\mathrm{h} 2}=\frac{Z}{2} \frac{I}{R} \frac{S_{a 2}}{g}=\frac{0.36}{2} \frac{1}{5} 2.5=0.09$
Similarly $\mathrm{A}_{\mathrm{h} 3}=0.09, \mathrm{~A}_{\mathrm{h} 4}=0.09$

The average response acceleration coefficient for rock sites as per IS 1893 (Part 1): 2002 is calculated as follows:

For rocky, or hard soil sites
$\frac{S_{a}}{g}=\left\{\begin{array}{cc}1+1.5 T ; & 0.00 \leq T \leq 0.10 \\ 2.5 ; & 0.10 \leq T \leq 0.40 \\ 1.00 / T ; & 0.40 \leq T \leq 4.0\end{array}\right\}$

For $\mathrm{T}_{1}=0.6978 \Rightarrow \frac{S_{a 1}}{g}=1.433$
For $\mathrm{T}_{2}=0.2450 \Rightarrow \frac{S_{a 2}}{g}=2.5$

For $\mathrm{T}_{3}=0.1636 \Rightarrow \frac{S_{a 3}}{g}=2.5$

For $\mathrm{T}_{4}=0.1382 \Rightarrow \frac{S_{a 4}}{g}=2.5$

## Design lateral force in each mode

$\mathrm{Q}_{\mathrm{i} 1}=\left(\mathrm{A}_{1} \mathrm{P}_{1} \Phi_{\mathrm{i} 1} \mathrm{~W}_{\mathrm{i}}\right)$
$\left[\mathrm{Q}_{\mathrm{i} 1}\right]=\left[\begin{array}{llll}\left(A_{h 1}\right. & P_{1} & \Phi_{11} & W_{1}\end{array}\right)$
$\left[\begin{array}{llll}((0.0515) & (-14.45) & (-0.0328) & (82.91 \times 9.81)) \\ ((0.0515) & (-14.45) & (-0.0608) & (82.91 \times 9.81)) \\ ((0.0515) & (-14.45) & (-0.0798) & (82.91 \times 9.81)) \\ ((0.0515) & (-14.45) & (-0.0872) & (50.57 \times 9.81))\end{array}\right]$
$=\left[\begin{array}{c}(19.852) \\ (36.8) \\ (48.3) \\ (32.192)\end{array}\right] \mathrm{kN}$
Similarly, $\left[\mathrm{Q}_{\mathrm{i}}\right]=\left[\begin{array}{c}23.62 \\ 19.13 \\ -8.11 \\ -15.68\end{array}\right],\left[\mathrm{Q}_{\mathrm{i} 3}\right]=\left[\begin{array}{c}12.42 \\ -8.30 \\ -6.88 \\ 7.86\end{array}\right],\left[\mathrm{Q}_{\mathrm{i} 4}\right]=\left[\begin{array}{c}1.511 \\ -2.62 \\ 3.04 \\ -1.615\end{array}\right]$

### 3.3.5 Step 5: Determination of storey shear forces in each mode

The peak shear force is given by,
$\mathrm{V}_{\mathrm{ik}}=\sum_{j=i+1}^{n} Q_{i k}$
The storey shear forces for the first mode is,
$\mathrm{v}_{\mathrm{ii1}}=\sum_{j=i+1}^{n} Q_{i 1}=\left[\begin{array}{l}V_{11} \\ V_{21} \\ V_{31} \\ V_{41}\end{array}\right]=\left[\begin{array}{c}\left(Q_{11}+Q_{21}+Q_{31}+Q_{41}\right) \\ \left(Q_{21}+Q_{31}+Q_{41}\right) \\ \left(Q_{31}+Q_{41}\right) \\ \left(Q_{41}\right)\end{array}\right]=\left[\begin{array}{c}137.144 \\ 117.292 \\ 80.492 \\ 32.192\end{array}\right] \mathrm{kN}$
Similarly,
$\mathrm{V}_{\mathrm{i} 2}=\left[\begin{array}{c}18.96 \\ -4.66 \\ -23.79 \\ -15.68\end{array}\right], \mathrm{V}_{\mathrm{i} 3}=\left[\begin{array}{c}5.1 \\ -7.32 \\ 0.98 \\ 7.86\end{array}\right], \mathrm{V}_{\mathrm{i} 4}=\left[\begin{array}{c}0.316 \\ -1.195 \\ 1.425 \\ -1.615\end{array}\right]$

### 3.3.6 Step 6: Determination of storey shear force due to all modes

The peak storey force $\left(\mathrm{V}_{1}\right)$ in storey i due to all modes considered is obtained by combining those due to each mode in accordance with modal combination i.e. SRSS (Square Root of Sum of Squares) or CQC (Complete Quadratic Combination) methods.

## Square root of sum of squares (SRSS)

If the building does not have closely spaced modes, the peak response quality ( $\lambda$ ) due to all modes considered shall be obtained as,
$\lambda=\sqrt{\sum_{k=1}^{r}\left(\lambda_{k}\right)^{2}}$,
where,
$\lambda_{\mathrm{k}}=$ Absolute value of quantity in mode ' k ', and r is the numbers of modes being considered
Using the above method, the storey shears are,
$\mathrm{V}_{1}=\left[\left(\mathrm{V}_{11}\right)^{2}+\left(\mathrm{V}_{12}\right)^{2}+\left(\mathrm{V}_{13}\right)^{2}+\left(\mathrm{V}_{14}\right)^{2}\right]^{1 / 2}$

$$
=\left[(137.144)^{2}+(18.96)^{2}+(5.1)^{2}+(0.316)^{2}\right]^{12}=138.54 \mathrm{kN}
$$

$\mathrm{V}_{2}=\left[\left(\mathrm{V}_{21}\right)^{2}+\left(\mathrm{V}_{22}\right)^{2}+\left(\mathrm{V}_{23}\right)^{2}+\left(\mathrm{V}_{24}\right)^{2}\right]^{1 / 2}$

$$
=\left[(117.292)^{2}+(-4.66)^{2}+(-7.32)^{2}+(-1.195)^{2}\right]^{12}=117.61 \mathrm{kN}
$$

$\mathrm{V}_{3}=\left[\left(\mathrm{V}_{31}\right)^{2}+\left(\mathrm{V}_{32}\right)^{2}+\left(\mathrm{V}_{33}\right)^{2}+\left(\mathrm{V}_{34}\right)^{2}\right]^{1 / 2}$

$$
=\left[(80.492)^{2}+(-23.79)^{2}+(0.98)^{2}+(1.425)^{2}\right]^{112}=83.95 \mathrm{kN}
$$

$\mathrm{V}_{4}=\left[\left(\mathrm{V}_{41}\right)^{2}+\left(\mathrm{V}_{42}\right)^{2}+\left(\mathrm{V}_{43}\right)^{2}+\left(\mathrm{V}_{44}\right)^{2}\right]^{1 / 2}$

$$
=\left[(32.192)^{2}+(-15.68)^{2}+(7.86)^{2}+(-1.615)^{2}\right]^{12}=36.69 \mathrm{kN}
$$

### 3.3.7 Step 7: Determination of lateral forces at each storey

The design lateral forces $\mathrm{F}_{\text {roof }}$ and $\mathrm{F}_{\mathrm{i}}$, at roof and the $\mathrm{i}^{\text {th }}$ floor, are calculated as,
$\mathrm{F}_{\text {roof }}=\mathrm{V}_{\text {roof }}$ and $\mathrm{F}_{\mathrm{i}}=\mathrm{V}_{\mathrm{i}}-\mathrm{V}_{\mathrm{i}+1}$

## Square root of sum of squares (SRSS)

$\mathrm{F}_{\text {roof }}=\mathrm{F}_{4}=\mathrm{V}_{4}=36.69 \mathrm{kN}$
$\mathrm{F}_{\text {floor } 3}=\mathrm{F}_{3}=\mathrm{V}_{3}-\mathrm{V}_{4}=83.95-36.69=47.26 \mathrm{kN}$
$\mathrm{F}_{\text {floor } 2}=\mathrm{F}_{2}=\mathrm{V}_{2}-\mathrm{V}_{3}=117.61-83.95=33.66 \mathrm{kN}$
$\mathrm{F}_{\text {floor } 1}=\mathrm{F}_{1}=\mathrm{V}_{1}-\mathrm{V}_{2}=138.54-117.61=20.93 \mathrm{kN}$

## B:Frame considering the stiffness of infills

The frame considered in previous section is again analysed by considering the stiffness of infill walls. The infill is modelled as equivalent diagonal strut.
The mass matrix [ M ] for the lumped plane frame model is
$\mathrm{M}=\left[\begin{array}{cccc}M_{1} & 0 & 0 & 0 \\ 0 & M_{2} & 0 & 0 \\ 0 & 0 & M_{3} & 0 \\ 0 & 0 & 0 & M_{4}\end{array}\right]=\left[\begin{array}{cccc}82.91 & 0 & 0 & 0 \\ 0 & 82.91 & 0 & 0 \\ 0 & 0 & 82.91 & 0 \\ 0 & 0 & 0 & 50.57\end{array}\right]$ ton
Column stiffness of storey,
$\mathrm{k}=12 \mathrm{EI} / \mathrm{L}^{3}=\left(12 \times 22360 \times 10^{3} \times\left(0.3 \times 0.5^{3} / 12\right)\right) / 3.5^{3}=19556.85 \mathrm{kN} / \mathrm{m}$
Stiffness of infill is determined by modelling the infill as an equivalent diagonal strut in which
Width of strut, $\quad \mathrm{W}=\frac{1}{2} \sqrt{\alpha_{h}{ }^{2}+\alpha_{l}{ }^{2}}$
$\alpha_{\mathrm{h}}=\frac{\Pi}{2}\left[\frac{E_{f} I_{c} h}{2 E_{m} t \sin 2 \theta}\right]^{\frac{1}{4}}, \alpha_{\mathrm{l}}=\Pi\left[\frac{E_{f} I_{b} l}{E_{m} t \sin 2 \theta}\right]^{\frac{1}{4}}, \theta=\tan ^{-1} \frac{h}{l}$
Where,
$\mathrm{E}_{\mathrm{f}}=$ Elastic modulus of frame material $=22360 \mathrm{~N} / \mathrm{m}^{2}$
$\mathrm{E}_{\mathrm{m}}=$ Elastic modulus of masonry wall $=13800 \mathrm{~N} / \mathrm{m}^{2}$
$t=$ Thickness of infill wall $=300 \mathrm{~mm}$
$h=$ Height of infill wall $=3.5 \mathrm{~m}$
I = Length of infill wall $=5 \mathrm{~m}$
$\mathrm{I}_{\mathrm{c}}=$ Moment of inertia of columns $=\frac{.3 \times .5^{3}}{12}=0.003125 \mathrm{~m}^{4}$
$I_{b}=$ Moment of inertia of beams $=\frac{.3 \times .45^{3}}{12}=0.002278 \mathrm{~m}^{4}$
$\alpha_{\mathrm{h}}=\frac{\Pi}{2}\left[\frac{22360 \times 0.003125 \times 3.5}{2 \times 13800 \times 0.3 \times \sin 2(35)}\right]^{\frac{1}{4}}=0.69 \mathrm{~m}$
$\alpha_{1}=\Pi\left[\frac{22360 \times 0.002278 \times 5}{13800 \times 0.3 \times \sin 2(35)}\right]^{\frac{1}{4}}=1.66 \mathrm{~m}$
$\mathrm{W}=\frac{1}{2} \sqrt{\alpha_{h}{ }^{2}+\alpha_{l}{ }^{2}}=0.8988 \mathrm{~m}$
$\mathrm{A}=$ Cross sectional area of diagonal stiffness $=\mathrm{W} \times \mathrm{t}=0.8988 \times 0.3=0.2696 \mathrm{~m}^{2}$
$1_{d}=$ Diagonal length of strut $=\sqrt{h^{2}+l^{2}}=6.103 \mathrm{~m}$
Therefore, stiffness of infill is
$\frac{A E_{m}}{l_{d}} \cos ^{2} \theta=\frac{0.2696 \times 13800 \times 10^{6}}{6.103} 0.819^{2}=408905.929 \times 10^{3} \mathrm{~N} / \mathrm{m}$

For the frame with two bays there are two struts participating in one direction, total lateral stiffness of each storey
$\mathrm{k}_{1}=\mathrm{k}_{2}=\mathrm{k}_{3}=\mathrm{k}_{4}=3 \times 19556.85+2 \times 408905929=817870.5286 \mathrm{kN} / \mathrm{m}$
Stiffness matrix [K] of lumped mass model is,
$\mathrm{K}=\left[\begin{array}{cccc}k_{1}+k_{2} & -k_{2} & 0 & 0 \\ -k_{2} & k_{2}+k_{3} & -k_{3} & 0 \\ 0 & -k_{3} & k_{3}+k_{4} & -k_{4} \\ 0 & 0 & -k_{4} & k_{4}\end{array}\right]=$
$\left[\begin{array}{cccc}1.6357 & -0.8178 & 0 & 0 \\ -0.8178 & 1.6357 & -0.8178 & 0 \\ 0 & -0.8178 & 1.6357 & -0.8178 \\ 0 & 0 & -0.8178 & 0.8178\end{array}\right] \times 10^{6} \mathrm{kN} / \mathrm{m}$

For the above stiffness and mass matrices, eigenvalues and eigenvectors are,
$\left|K-\omega^{2} m\right|=\left|\begin{array}{cccc}2 k-\omega^{2} m & -k_{2} & 0 & 0 \\ -k_{2} & 2 k-\omega^{2} m & -k_{3} & 0 \\ 0 & -k_{3} & 2 k-\omega^{2} m & -k_{4} \\ 0 & 0 & -k 4 & k-\omega^{2} m\end{array}\right|=0, \mathrm{k} / \mathrm{m}=\omega_{\mathrm{n}}{ }^{2}$
Therefore, quadratic equation is,
$\left(\omega_{\mathrm{n}}^{2}\right)^{4}-8.3\left(\omega_{\mathrm{n}}^{2}\right)^{3}\left(\omega^{2}\right)+10.75\left(\omega_{\mathrm{n}}^{2}\right)^{2}\left(\omega^{2}\right)^{2}-4.45\left(\omega_{\mathrm{n}}^{2}\right)\left(\omega^{2}\right)^{3}+0.575\left(\omega^{2}\right)^{4}=0$

Eigenvalues
$\left[\omega^{2}\right]=\left[\begin{array}{llll}1442 & & & \\ & 11698 & & \\ & & 26227 & \\ & & & 36719\end{array}\right]$
$\omega_{1}{ }^{2}=1442, \omega_{2}{ }^{2}=11698, \omega_{3}{ }^{2}=26227, \omega_{4}{ }^{2}=36719$
Eigenvectors $\{\boldsymbol{\Phi}\}$
$\{\Phi\}=\left\{\Phi_{1} \Phi_{2} \Phi_{3} \Phi_{4}\right\}=\left[\begin{array}{cccc}-0.0328 & 0.0795 & 0.0808 & -0.0397 \\ -0.0608 & 0.0644 & -0.0540 & 0.0690 \\ -0.0798 & -0.0273 & -0.0448 & -0.0799 \\ -0.0872 & -0.0865 & 0.0839 & 0.0696\end{array}\right]$
Natural frequency in various modes
$[\omega]=\left[\begin{array}{cccc}37.975 & 0 & 0 & 0 \\ 0 & 108.157 & 0 & 0 \\ 0 & 0 & 161.947 & 0 \\ 0 & 0 & 0 & 191.621\end{array}\right] \mathrm{rad} / \mathrm{s}$
Natural time period
$\mathrm{T}=\left[\begin{array}{cccc}0.1655 & 0 & 0 & 0 \\ 0 & 0.0581 & 0 & 0 \\ 0 & 0 & 0.0388 & 0 \\ 0 & 0 & 0 & 0.0328\end{array}\right] \mathrm{s}$
Modal Participation Factors
$\mathrm{p}_{\mathrm{k}}=\frac{\sum_{i=1}^{n} W_{i} \phi_{i k}}{\sum_{i=1}^{n} W_{i}\left(\phi_{i k}\right)^{2}}$
$\mathrm{p}_{1}=\frac{\sum_{i=1}^{4} W_{i} \phi_{i 1}}{\sum_{i=1}^{4} W_{i}\left(\phi_{i 1}\right)^{2}}=\frac{\left(W_{1} \phi_{11}+W_{2} \phi_{21}+W_{3} \phi_{31}+W_{4} \phi_{41}\right)}{\left(W_{1}\left(\phi_{11}\right)^{2}+W_{2}\left(\phi_{21}\right)^{2}+W_{3}\left(\phi_{31}\right)^{2}+W_{4}\left(\phi_{41}\right)^{2}\right)}=-14.45$
$\mathrm{p}_{2}=\frac{\sum_{i=1}^{4} W_{i} \phi_{i 2}}{\sum_{i=1}^{4} W_{i}\left(\phi_{i 2}\right)^{2}}=\frac{\left(W_{1} \phi_{12}+W_{2} \phi_{22}+W_{3} \phi_{32}+W_{4} \phi_{42}\right)}{\left(W_{1}\left(\phi_{12}\right)^{2}+W_{2}\left(\phi_{22}\right)^{2}+W_{3}\left(\phi_{32}\right)^{2}+W_{4}\left(\phi_{42}\right)^{2}\right)}=4.06$
Similarly,
$\mathrm{p}_{3}=2.1, \mathrm{p}_{4}=-0.52$

## Modal Mass

$\mathrm{M}_{\mathrm{k}}=\frac{\left[\sum_{i=1}^{n} W_{i} \phi_{i k}\right]^{2}}{g\left[\sum_{i=1}^{n} W_{i}\left(\phi_{i k}\right)^{2}\right]}$
$\mathrm{M}_{1}=\frac{\left[\sum_{i=1}^{4} W_{i} \phi_{i 1}\right]^{2}}{g\left[\sum_{i=1}^{4} W_{i}\left(\phi_{i 1}\right)^{2}\right]}$
$\mathrm{M}_{1}$

$$
[9.81(82.91(-0.0328)+82.91(-0.0608)+82.91(-0.0798)+50.57(-0.0872))]^{2}
$$

$9.81\left[9.81\left(82.91(-0.0328)^{2}+82.91(-0.0608)^{2}+82.91(-0.0798)^{2}+50.57(-0.0872)^{2}\right)\right]$
$=269.85$
$\mathrm{M}_{2}=\frac{\left[\sum_{i=1}^{4} W_{i} \phi_{i 2}\right]^{2}}{g\left[\sum_{i=1}^{4} W_{i}\left(\phi_{i 2}\right)^{2}\right]}$, similarly, $\mathrm{M}_{2}=21.42, \mathrm{M}_{3}=5.78, \mathrm{M}_{4}=0.34$

Modal contributions of various modes
For mode $1, \frac{M_{1}}{M}=\frac{269.85}{299.3}=0.90=90 \%$
For mode 2, $\frac{M_{2}}{M}=\frac{21.42}{299.3}=0.0715=7.15 \%$
For mode 3, $\frac{M_{3}}{M}=\frac{5.78}{299.3}=0.0193=1.93 \%$
For mode $4, \frac{M_{4}}{M}=\frac{0.34}{299.3}=0.0011=0.11 \%$

## Design lateral force at each floor in each mode

The design lateral force $\left(\mathrm{Q}_{\mathrm{ik}}\right)$ at floor i in mode k is given by,
$\mathrm{Q}_{\mathrm{ik}}=\mathrm{A}_{\mathrm{k}} \Phi_{\mathrm{ik}} \mathrm{P}_{\mathrm{k}} \mathrm{W}_{\mathrm{i}}$
The design horizontal seismic coefficient $\mathrm{A}_{\mathrm{h}}$ for various modes are,
$\mathrm{A}_{\mathrm{hk}}=\frac{Z}{2} \frac{I}{R} \frac{S_{a k}}{g}$
$\mathrm{A}_{\mathrm{h} 1}=\frac{Z}{2} \frac{I}{R} \frac{S_{a 1}}{g}=\frac{0.36}{2} \frac{1}{5} 2.5=0.090$
$\mathrm{A}_{\mathrm{h} 2}=\frac{Z}{2} \frac{I}{R} \frac{S_{a 2}}{g}=\frac{0.36}{2} \frac{1}{5} 1.871=0.067$
Similarly $\mathrm{A}_{\mathrm{h} 3}=0.056, \mathrm{~A}_{\mathrm{h} 4}=0.053$
The average response acceleration coefficient for rock sites as per IS 1893 (Part 1): 2002 is calculated as follows:

For rocky, or hard soil sites
$\frac{S_{a}}{g}=\left\{\begin{array}{cc}1+1.5 T ; & 0.00 \leq T \leq 0.10 \\ 2.5 ; & 0.10 \leq T \leq 0.40 \\ 1.00 / T ; & 0.40 \leq T \leq 4.0\end{array}\right\}$

For $\mathrm{T}_{1}=0.1655 \Rightarrow \frac{S_{a 1}}{g}=2.5$
For $\mathrm{T}_{2}=0.0581 \Rightarrow \frac{S_{a 2}}{g}=1+15 \mathrm{~T}=1.871$
For $\mathrm{T}_{3}=0.0388 \Rightarrow \frac{S_{a 3}}{g}=1+15 \mathrm{~T}=1.582$
For $\mathrm{T}_{4}=0.1382 \Rightarrow \frac{S_{a 4}}{g}=1+15 \mathrm{~T}=1.49$

## Design lateral force in each mode

$\mathrm{Q}_{\mathrm{i} 1}=\left(\mathrm{A}_{1} \mathrm{P}_{1} \Phi_{\mathrm{i} 1} \mathrm{~W}_{\mathrm{i}}\right)$
$\left[\mathrm{Q}_{\mathrm{i} 1}\right]=\left[\begin{array}{llll}\left(A_{h 1}\right. & P_{1} & \Phi_{11} & W_{1}\end{array}\right)$
$\left[\begin{array}{llll}((0.090) & (-14.45) & (-0.0328) & (82.91 \times 9.81)) \\ ((0.090) & (-14.45) & (-0.0608) & (82.91 \times 9.81)) \\ ((0.090) & (-14.45) & (-0.0798) & (82.91 \times 9.81)) \\ ((0.090) & (-14.45) & (-0.0872) & (50.57 \times 9.81))\end{array}\right]$
$=\left[\begin{array}{l}(34.69) \\ (64.31) \\ (84.40) \\ (56.25)\end{array}\right] \mathrm{kN}$
Similarly, $\left[\mathrm{Q}_{\mathrm{i} 2}\right]=\left[\begin{array}{c}17.58 \\ 14.24 \\ -6.04 \\ -11.67\end{array}\right],\left[\mathrm{Q}_{\mathrm{i} 3}\right]=\left[\begin{array}{c}7.728 \\ -5.16 \\ -4.28 \\ 4.89\end{array}\right],\left[\mathrm{Q}_{\mathrm{i} 4}\right]=\left[\begin{array}{c}0.88 \\ -1.54 \\ 1.79 \\ -0.95\end{array}\right]$

Storey shear forces in each mode
The peak shear force is given by,
$\mathrm{V}_{\mathrm{ik}}=\sum_{j=i+1}^{n} Q_{i k}$

The storey shear forces for the first mode is,
$\mathrm{V}_{\mathrm{i} 1}=\sum_{j=i+1}^{n} Q_{i 1}=\left[\begin{array}{l}V_{11} \\ V_{21} \\ V_{31} \\ V_{41}\end{array}\right]=\left[\begin{array}{c}\left(Q_{11}+Q_{21}+Q_{31}+Q_{41}\right) \\ \left(Q_{21}+Q_{31}+Q_{41}\right) \\ \left(Q_{31}+Q_{41}\right) \\ \left(Q_{41}\right)\end{array}\right]=\left[\begin{array}{c}239.65 \\ 204.96 \\ 140.65 \\ 56.25\end{array}\right] \mathrm{kN}$
Similarly,
$\mathrm{V}_{\mathrm{i} 2}=\left[\begin{array}{c}14.11 \\ -3.47 \\ -17.71 \\ -11.67\end{array}\right], \mathrm{V}_{\mathrm{i} 3}=\left[\begin{array}{c}3.178 \\ -4.55 \\ 0.61 \\ 4.89\end{array}\right], \mathrm{V}_{\mathrm{i} 4}=\left[\begin{array}{c}0.18 \\ -0.7 \\ 0.84 \\ -0.95\end{array}\right]$

## Storey shear force due to all modes

Square root of sum of squares (SRSS)

$$
\begin{aligned}
\mathrm{V}_{1} & =\left[\left(\mathrm{V}_{11}\right)^{2}+\left(\mathrm{V}_{12}\right)^{2}+\left(\mathrm{V}_{13}\right)^{2}+\left(\mathrm{V}_{14}\right)^{2}\right]^{1 / 2} \\
& =\left[(239.65)^{2}+(14.11)^{2}+(3.178)^{2}+(0.18)^{2}\right]^{112}=240.08 \mathrm{kN} \\
\mathrm{~V}_{2} & =\left[\left(\mathrm{V}_{21}\right)^{2}+\left(\mathrm{V}_{22}\right)^{2}+\left(\mathrm{V}_{23}\right)^{2}+\left(\mathrm{V}_{24}\right)^{2}\right]^{1 / 2} \\
= & {\left[(204.96)^{2}+(-3.47)^{2}+(-4.55)^{2}+(-0.7)^{2}\right]^{112}=205.04 \mathrm{kN} } \\
\mathrm{~V}_{3} & =\left[\left(\mathrm{V}_{31}\right)^{2}+\left(\mathrm{V}_{32}\right)^{2}+\left(\mathrm{V}_{33}\right)^{2}+\left(\mathrm{V}_{34}\right)^{2}\right]^{1 / 2} \\
& =\left[(140.65)^{2}+(-17.71)^{2}+(0.61)^{2}+(0.84)^{2}\right]^{112}=141.76 \mathrm{kN}
\end{aligned}
$$

$\mathrm{V}_{4}=\left[\left(\mathrm{V}_{41}\right)^{2}+\left(\mathrm{V}_{42}\right)^{2}+\left(\mathrm{V}_{43}\right)^{2}+\left(\mathrm{V}_{44}\right)^{2}\right]^{1 / 2}$

$$
=\left[(56.25)^{2}+(-11.67)^{2}+(4.89)^{2}+(-0.95)^{2}\right]^{12}=57.66 \mathrm{kN}
$$

## Lateral forces at each storey due to all modes

Square root of sum of squares (SRSS)
$\mathrm{F}_{\text {roof }}=\mathrm{F}_{4}=\mathrm{V}_{4}=57.66 \mathrm{kN}$
$\mathrm{F}_{\text {floor } 3}=\mathrm{F}_{3}=\mathrm{V}_{3}-\mathrm{V}_{4}=141.76-57.66=84.1 \mathrm{kN}$
$\mathrm{F}_{\text {floor } 2}=\mathrm{F}_{2}=\mathrm{V}_{2}-\mathrm{V}_{3}=205.04-141.76=63.28 \mathrm{kN}$
$\mathrm{F}_{\text {floorl }}=\mathrm{F}_{1}=\mathrm{V}_{1}-\mathrm{V}_{2}=240.08-205.04=35.04 \mathrm{kN}$

Table 3.2: Comparison of lateral forces by static and dynamic analysis

|  | By Equivalent Static Lateral <br> Force Method (kN) | By Response Spectrum Method |  |  |
| :--- | :--- | :--- | :--- | :---: |
|  | By not considering the <br> stiffness of infills (kN) | By considering the <br> stiffness of infills (kN) |  |  |
| Roof | 79.96 | 36.69 | 57.66 |  |
| $3^{\text {rd }}$ Floor | 73.75 | 47.26 | 84.1 |  |
| $2^{\text {nd }}$ Floor | 32.78 | 33.66 | 63.28 |  |
| $1^{\text {st }}$ Floor | 8.19 | 20.93 | 35.04 |  |

From the above results it was conclude that the value of forces that building can take are coming less in dynamic analysis as compared to static analysis. This shows that if we design building using dynamic analysis though we have to perform more calculations but it give more precise results as compared. So we can say that dynamic analysis is economic

> Chapter 4 Seismic Analysis by Staad Pro

### 4.1 About Staad Pro

STAAD or (STAAD.Pro) is a structural analysis and design computer program originally developed by Research Engineers International at Yorba Linda, CA in year 1997. In late 2005, Research Engineers International was bought by Bentley Systems. An older version called Staad-III for windows is used by Iowa State University for educational purposes for civil and structural engineers. Initially it was used for DOS-Window system. The commercial version STAAD.Pro is one of the most widely used structural analysis and design software. It supports several steel, concrete and timber design codes. It can make use of various forms of analysis from the traditional 1st order static analysis, 2nd order p-delta analysis, geometric nonlinear analysis or a buckling analysis. It can also make use of various forms of dynamic analysis from modal extraction to time history and response spectrum analysis. In recent years it has become part of integrated structural analysis and design solutions mainly using an exposed API called OpenSTAAD to access and drive the program using an VB macro system included in the application or other by including OpenSTAAD functionality in applications that themselves include suitable programmable macro systems. Additionally STAAD.Pro has added direct links to applications such as RAM Connection and STAAD.Foundation to provide engineers working with those applications which handle design post processing not handled by STAAD.Pro itself. Another form of integration supported by STAAD.Pro is the analysis schema of the CIMsteel Integration Standard, version 2 commonly known as CIS/2 and used by a number modelling and analysis applications.

### 4.2 Static Analysis

The above analysis done manually is done by staad pro below and results are obtained.

### 4.2.1 Source code

Staad Space
Start Job Information
Engineer Date 04-Apr-16
End Job Information
Input Width 79
Unit Meter Kn
Joint Coordinates
100 0; 2500 0; 3100 0; 403.50 0; 553.5 0; $6103.50 ; 7070 ; 8570$ 0;
$91070 ; 10010.50 ; 11510.50 ; 121010.50 ; 130140 ; 145140$;
$1510140 ; 16002.5 ; 17502.5$; 18100 2.5; 1903.5 2.5; 2053.5 2.5;
21103.5 2.5; $22072.5 ; 23572.5 ; 241072.5 ; 25010.52 .5$;
$26510.52 .5 ; 271010.52 .5 ; 280142.5 ; 295142.5 ; 3010142.5$;
$31005 ; 32505 ; 331005 ; 3403.55 ; 3553.55 ; 36103.55 ; 37075$;
$38575 ; 391075 ; 40010.55$ 5; 41510.5 5; 421010.5 5; 43014 5;
445145 5; 451014 5;
Member Incidences
14 5; 25 6; 37 8; 48 9; 510 11; 611 12; 713 14; 814 15; 914 4; 102 5;
113 6; 1247 ; 135 8; 146 9; 157 10; 168 11; 179 12; 1810 13; 1911 14;
2012 15; 2119 20; 2220 21; 2322 23; 2423 24; 2525 26; 2626 27; 272829 ;
2829 30; 2916 19; 3017 20; 3118 21; 3219 22; 332023 ; 3421 24; 352225 ;
3623 26; 3724 27; 3825 28; 3926 29; 4027 30; 4134 35; 4235 36; 433738 ;

```
44 38 39;4540 41; 46 41 42; 47 43 44;48 44 45; 49 31 34; 50 32 35; 51 33 36;
52 34 37; 53 35 38; 54 36 39;55 37 40;56 38 41; 57 39 42;58 40 43; 59 41 44;
6042 45;}614\mathrm{ 19; 62 5 20; 63 6 21; 64 7 22;}65 8 23;66 9 24; 67 10 25;
68 11 26; 69 12 27; 70 13 28; 71 14 29; 72 15 30; 73 19 34; 74 20 35; 75 21 36;
76 22 37; 77 23 38;78 24 39;79 25 40; 80 26 41; 81 27 42; 82 28 43; 83 29 44;
84 30 45;
Element Incidences Shell
85 131429 28; 86 28 4344 29; 87 29 30 45 44; 88 10 11 26 25; 89 11 12 27 26;
90 25 26 41 40; 91 26 27 42 41;927 8 23 22;93 22 37 38 23;94 23 24 39 38;
95 }8924\mathrm{ 23; 96 4520 19;97 5 621 20;98 1920 35 34; 99 20 21 36 35;
100141530 29;
Element Property
85 To 100 Thicknesses 0.15
Define Material Start
Isotropic Concrete
E 2.17185e+007
Poisson 0.17
Density 23.5616
Alpha 1e-005
Damp 0.05
Type Concrete
Strength Fcu 27579
End Define Material
Member Property American
9 To 20 29 To 40 49 To 60 Pris Yd 0.5 Zd 0.3
61 To }84\mathrm{ Pris Yd 0.45 Zd 0.3
1 To 8 21 To 28 41 To 48 Pris Yd 0.4 Zd 0.3
Constants
Material Concrete All
Supports
1 To 3 16 To }1831\mathrm{ To 33 Fixed
Define 1893 Load
Zone 0.36 Rf 5 I 1 Ss 1 St 1
Selfweight }
Floor Weight
Yrange 00 Fload 1.75 Xrange 3.5 10 Zrange 0 0
Load 1 Loadtype Seismic Title El X +Ve
1893 Load X 1
Load 2 Loadtype Seismic Title El X -Ve
1893 Load X -1
Load 3 Loadtype Seismic Title El Z+Ve
1893 Load Z 1
Load 4 Loadtype Seismic Title El Z-Ve
1893 Load Z -1
Load 5 Loadtype Dead Title Dl
Selfweight Y -1
Member Load
1 To 8 21 To 28 41 To 48 61 To 84 Uni Gy -56
Load 6 Loadtype Live Title Ll
Floor Load
Yrange 3.5 10.5 Fload -1.75 Gy
Load Comb 7 1.5(Dl + Ll +El X+Ve)
11.551.561.5
Load Comb 8 1.5(Dl + Ll +El Z+Ve)
```

31.551 .561 .5

Load Comb 9 1.2(Dl + Ll -El X-Ve)
$51.261 .22-1.2$
Load Comb 10 1.2(Dl + Ll -El Z-Ve)
51.261 .24 -1.2

Perform Analysis
Perform Analysis Print Statics Check
Load List 7 To 10
Print Joint Displacements List All
Print Member Forces List All
Print Support Reaction List 1 To 316 To 1831 To 33
Print Story Drift
Print Analysis Results
Finish

### 4.2.2 Results

### 4.2.2.1

Table 4.1: Beam member forces

| Beam no. | Max. moment in $\mathbf{Z}$ direction $\left(\mathbf{M}_{\mathbf{z}}\right)$ (kNm) | Max. shear force (kN) |
| :---: | :---: | :---: |
| 1 | 215.2 | 239.92 |
| 2 | 198.23 | 232.11 |
| 3 | 208.33 | 236.89 |
| 4 | 207.71 | 235.74 |
| 5 | 196.88 | 231.85 |
| 6 | 209.1 | 236.12 |
| 7 | 192.8 | 229.21 |
| 8 | 184.43 | 225.53 |
| 21 | 217.87 | 244.79 |
| 22 | 201.99 | 237.28 |
| 23 | 210.68 | 241.59 |
| 24 | 212.18 | 241.14 |
| 25 | 199.96 | 236.87 |
| 26 | 213.94 | 241.71 |
| 27 | 189.03 | 227.46 |
| 28 | 182.26 | 224.42 |
| 41 | 215.2 | 239.92 |
| 42 | 198.23 | 232.11 |
| 43 | 208.33 | 236.89 |
| 44 | 207.71 | 235.74 |
| 45 | 196.88 | 231.85 |
| 46 | 209.1 | 236.12 |
| 47 | 192.8 | 229.21 |
| 48 | 184.43 | 225.63 |
| 61 | 252.33 | 141.5 |
| 62 | 242.73 | 137.78 |
| 63 | 252.33 | 141.5 |
| 64 | 233.64 | 132.34 |
| 65 | 222.78 | 128 |
| 66 | 233.64 | 132.34 |
| 67 | 223.605 | 123.37 |


| 68 | 228.36 | 127.82 |
| :---: | :---: | :---: |
| 69 | 221.85 | 123.34 |
| 70 | 205.335 | 115.86 |
| 71 | 205.14 | 117.08 |
| 72 | 204.33 | 116.14 |
| 73 | 264.105 | 137.92 |
| 74 | 255.345 | 135.27 |
| 75 | 264.105 | 137.92 |
| 76 | 270.69 | 143.7 |
| 77 | 265.14 | 142.53 |
| 78 | 270.69 | 143.7 |
| 79 | 263.22 | 141.83 |
| 80 | 261.765 | 142.66 |
| 81 | 263.22 | 141.83 |
| 82 | 221.775 | 123.54 |
| 83 | 218.775 | 122.99 |
| 84 | 221.75 | 123.54 |

### 4.2.2.2

Table 4.2: Column member forces

| Column no. | Max. moment in Z direction $\left(\mathbf{M}_{\mathbf{z}}\right)$ (kNm) | Max. moment in $Y$ direction ( $\mathbf{M}_{\mathbf{y}}$ ) (kNm) | Max. shear force ( $\mathbf{P}_{\mathbf{u}}$ ) (kN) |
| :---: | :---: | :---: | :---: |
| 9 | 65.72 | 27.71 | 1461.79 |
| 10 | 47.53 | 28.18 | 2528.01 |
| 11 | 83.82 | 27.71 | 1551.8 |
| 12 | 93.2 | 19.04 | 1109.05 |
| 13 | 42.51 | 21.57 | 1897.6 |
| 14 | 120.4 | 21.74 | 1171.93 |
| 15 | 85.38 | 22.19 | 741.4 |
| 16 | 37.21 | 24.27 | 1263.47 |
| 17 | 107.21 | 24.69 | 775.48 |
| 18 | 148.25 | 29.22 | 359.68 |
| 19 | 27.07 | 32.12 | 628.44 |
| 20 | 165.48 | 31.42 | 371.26 |
| 29 | 68.91 | 37.76 | 1960.17 |
| 30 | 50.32 | 38.4 | 3033.68 |
| 31 | 87.99 | 37.76 | 2022.94 |
| 32 | 97.35 | 38.75 | 1453.15 |
| 33 | 51.02 | 40.57 | 2231.64 |
| 34 | 126.12 | 38.75 | 1495.34 |
| 35 | 87.59 | 32.64 | 959.09 |
| 36 | 44.04 | 34.02 | 1474.06 |
| 37 | 110.88 | 32.64 | 980.68 |
| 38 | 143.39 | 20.36 | 472.36 |
| 39 | 25.35 | 20.92 | 747.39 |
| 40 | 161.61 | 20.36 | 479.12 |
| 49 | 57.34 | 39.36 | 1610.4 |
| 50 | 47.53 | 41.02 | 2641.98 |
| 51 | 83.82 | 39.36 | 1610.4 |
| 52 | 101.21 | 47.18 | 1208.6 |
| 53 | 42.51 | 50.69 | 1972.25 |


| 54 | 120.4 | 47.18 | 1208.6 |
| :---: | :---: | :---: | :---: |
| 55 | 91.77 | 47.05 | 793.17 |
| 56 | 37.21 | 49.66 | 1301.25 |
| 57 | 107.21 | 47.05 | 793.17 |
| 58 | 152.16 | 45.41 | 375.5 |
| 59 | 27.07 | 48.13 | 639.19 |
| 60 | 165.48 | 45.41 | 375.5 |

### 4.3 Response Spectrum Analysis

The above analysis done manually is done by staad pro below and results are obtained.

### 4.3.1 Source code

Staad Space
Start Job Information
Engineer Date 04-Apr-16
End Job Information
Input Width 79
Unit Meter Kn
Joint Coordinates
$1000 ; 2500 ; 31000 ; 403.50 ; 553.5$ 0; $6103.50 ; 7070 ; 8570$ 0;
91070 ; 10010.50 ; 11510.50 ; 121010.50 ; 130140 ; 145140 ;
$1510140 ; 16002.5 ; 17502.5$; 18100 2.5; 1903.5 2.5; 2053.5 2.5;
2110 3.5 2.5; $22072.5 ; 23572.5 ; 241072.5 ; 25010.5$ 2.5;
$26510.52 .5 ; 271010.52 .5 ; 280142.5$; 295142.5 ; 3010142.5 ;
$31005 ; 32505 ; 331005 ; 3403.5$ 5; 3553.5 5; 36103.5 5; 37075 ;
$38575 ; 391075$ 5; 40010.5 5; 41510.5 5; 421010.5 5; 43014 5;
445145 5; 451014 5;
Member Incidences
14 5; 25 6; 37 8; 48 9; 510 11; 611 12; 713 14; 814 15; 914 ; 102 5;
113 6; 124 7; 135 8; 146 9; 157 10; 168 11; 179 12; 1810 13; 1911 14;
2012 15; 2119 20; 2220 21; 2322 23; 2423 24; 25 25 26; 2626 27; 272829 ;
2829 30; 2916 19; 3017 20; 3118 21; $321922 ; 332023 ; 3421$ 24; 352225 ;
3623 26; 3724 27; 3825 28; 3926 29; 4027 30; 4134 35; 4235 36; 4337 38;
4438 39; 4540 41; 4641 42; 4743 44; 4844 45; 49 31 34; 5032 35; 5133 36;
5234 37; 5335 38; 5436 39; 5537 40; 5638 41; 5739 42; 5840 43; 5941 44;
6042 45; 614 19; 625 20; 636 21; 647 22; 658 23; 669 24; 6710 25;
6811 26; 6912 27; 7013 28; 7114 29; 7215 30; 73 19 34; 7420 35; 7521 36;
7622 37; 7723 38; 7824 39; 7925 40; 8026 41; 8127 42; 8228 43; 8329 44;
8430 45;
Element Incidences Shell
85131429 28; 86284344 29; 87293045 44; 88101126 25; 89111227 26;
90252641 40; 91262742 41; 927823 22; 93223738 23; 94232439 38;
958924 23; 964520 19; 975621 20; 98192035 34; 99202136 35;
100141530 29;
Element Property
85 To 100 Thicknesses 0.15
Define Material Start
Isotropic Concrete
E 2.17185e+007
Poisson 0.17

Density 23.5616
Alpha 1e-005
Damp 0.05
Type Concrete
Strength Fcu 27579
End Define Material
Member Property American
9 To 2029 To 4049 To 60 Pris Yd 0.5 Zd 0.3
61 To 84 Pris Yd 0.45 Zd 0.3
1 To 821 To 2841 To 48 Pris Yd 0.4 Zd 0.3
Constants
Material Concrete All
Supports
1 To 316 To 1831 To 33 Fixed
Define 1893 Load
Zone 0.36 Rf 5 I 1 Ss 1 St 1
Selfweight 1
Floor Weight
Yrange 3.5 10.5 Fload 1.75
Load 1 Loadtype Live Title Load Case 1 Live
Floor Load
Yrange 3.5 10.5 Fload -1.75 Gy
Load 2 Loadtype Seismic Title Load Case 3 Rs
Self-weight X 1
Selfweight Y 1
Selfweight Z 1
Member Load
1 To 84 Uni Gx 56
1 To 84 Uni Gz 56
Floor Load
Yrange 00 Fload 1.75 Gx
Yrange 00 Fload 1.75 Gy
Yrange 00 Fload 1.75 Gz
Spectrum Srss 1893 X 0.036 Acc Damp 0.05
Soil Type 1
Load 3 Loadtype Dead Title Load Case 2 Dead
Selfweight Y-1
Member Load
1 To 84 Uni Gy -56
Perform Analysis
Perform Analysis Print Mode Shapes
Print Analysis Results
Finish

### 4.3.2 Results

### 4.3.2.1

Table 4.3: Beam member forces

| Beam no. | Max. moment in $\mathbf{Z}$ direction ( $\mathbf{M}_{\mathbf{z}}$ ) (kNm) | Max. shear force (kN) |
| :---: | :---: | :---: |
| 1 | 124.7 | 149.57 |
| 2 | 124.7 | 149.57 |
| 3 | 119.69 | 147.42 |
| 4 | 119.69 | 147.42 |
| 5 | 123.07 | 148.55 |
| 6 | 123.07 | 148.55 |
| 7 | 123.3 | 150.52 |
| 8 | 123.3 | 150.52 |
| 21 | 124.34 | 149.39 |
| 22 | 124.34 | 149.39 |
| 23 | 119.15 | 147.15 |
| 24 | 119.15 | 147.15 |
| 25 | 123.79 | 148.79 |
| 26 | 123.79 | 148.79 |
| 27 | 122.04 | 149.85 |
| 28 | 122.04 | 149.85 |
| 41 | 124.7 | 149.57 |
| 42 | 124.7 | 149.57 |
| 43 | 119.69 | 147.42 |
| 44 | 119.69 | 147.42 |
| 45 | 123.07 | 148.55 |
| 46 | 123.07 | 148.55 |
| 47 | 123.3 | 150.52 |
| 48 | 123.3 | 150.52 |
| 61 | 26.87 | 75.22 |
| 62 | 26.22 | 74.9 |
| 63 | 26.87 | 75.22 |
| 64 | 28.55 | 77.55 |
| 65 | 29.44 | 78.39 |
| 66 | 28.55 | 77.55 |
| 67 | 31.53 | 80.61 |
| 68 | 33.28 | 82 |
| 69 | 31.53 | 80.61 |
| 70 | 24.15 | 77.01 |
| 71 | 23.89 | 77.32 |
| 72 | 24.15 | 77.01 |
| 73 | 26.22 | 75.22 |
| 74 | 26.87 | 74.9 |
| 75 | 26.87 | 75.22 |
| 76 | 28.55 | 77.55 |
| 77 | 29.44 | 78.39 |
| 78 | 28.55 | 77.55 |
| 79 | 31.53 | 80.61 |
| 80 | 33.28 | 82 |


| 81 | 31.53 | 80.61 |
| :---: | :---: | :---: |
| 82 | 24.15 | 77.01 |
| 83 | 23.89 | 77.32 |
| 84 | 24.15 | 77.01 |

Table 4.4: Column member forces

| Column no. | Max. moment in Z direction $\left(M_{z}\right)$ (kNm) | Max. moment in $Y$ direction ( $\mathbf{M}_{\mathbf{y}}$ ) (kNm) | Max. shear force ( $\mathbf{P}_{\mathbf{u}}$ ) (kN) |
| :---: | :---: | :---: | :---: |
| 9 | 91.05 | 7.65 | 1770.69 |
| 10 | 104.96 | 7.99 | 2433.1 |
| 11 | 91.05 | 7.65 | 1770.69 |
| 12 | 62.67 | 13.16 | 1335.94 |
| 13 | 83.71 | 13.55 | 1828.45 |
| 14 | 62.67 | 13.16 | 1335.94 |
| 15 | 56.97 | 15.13 | 891.06 |
| 16 | 69.37 | 15.23 | 1221.59 |
| 17 | 56.97 | 15.13 | 891.06 |
| 18 | 99.39 | 19.77 | 438.92 |
| 19 | 52.18 | 20.68 | 614.33 |
| 20 | 99.39 | 19.77 | 438.92 |
| 29 | 95.08 | 37.76 | 2061.2 |
| 30 | 110.78 | 38.4 | 2746.93 |
| 31 | 95.08 | 37.76 | 2061.2 |
| 32 | 61.23 | 38.75 | 1537.44 |
| 33 | 99.49 | 40.57 | 2038.18 |
| 34 | 61.23 | 38.75 | 1537.44 |
| 35 | 54.9 | 32.64 | 1022.10 |
| 36 | 81.87 | 34.02 | 1357.55 |
| 37 | 54.9 | 32.64 | 1022.1 |
| 38 | 94.63 | 20.36 | 511.39 |
| 39 | 60.97 | 20.92 | 687.46 |
| 40 | 94.63 | 20.36 | 511.39 |
| 49 | 44.25 | 39.36 | 149.57 |
| 50 | 104.96 | 41.02 | 2433.1 |
| 51 | 91.05 | 39.36 | 1770.69 |
| 52 | 62.67 | 47.18 | 1335.94 |
| 53 | 83.71 | 50.69 | 1828.45 |
| 54 | 62.67 | 47.18 | 1335.94 |
| 55 | 56.97 | 47.05 | 891.06 |
| 56 | 69.37 | 49.66 | 1221.59 |
| 57 | 56.97 | 47.05 | 891.06 |
| 58 | 99.39 | 45.41 | 438.92 |
| 59 | 52.18 | 48.13 | 614.33 |
| 60 | 99.39 | 45.41 | 438.92 |

From the above results it was concluded that the member forces of building are coming less in dynamic analysis as compared to static analysis. This shows that if design of building is done using dynamic analysis though to perform more calculations but it give more precise results as compared. So it can be said that dynamic analysis is economic.

# Chapter 5 <br> Design of <br> beams and columns by spreadsheet 

### 5.1 Design of beams

Doubly reinforced beams are generally resorted to in situations where the cross-sectional dimensions of the beam are restricted and where singly reinforced sections are not adequate in terms of moment resisting capacity. Doubly reinforced beams are also used in situations where reversal of moments is likely. The presence of compression reinforcement reduces long term deflections due to shrinkage and creep. All compression reinforcement must be enclosed by closed stirrups in order to prevent their possible buckling and to provide some ductility by confinement of concrete.

### 5.2 Spreadsheet of design of doubly reinforced beam

## List of symbols

$\mathrm{b}=$ breadth of beam (mm)
$\mathrm{D}=$ depth of beam (mm)
$\mathrm{d}^{\prime}=$ effective depth of beam (mm)
$\mathrm{M}_{\mathrm{u}}=$ moment (kNm)
$\mathrm{A}_{\mathrm{st}}=$ area of steel in tension $\left(\mathrm{mm}^{2}\right)$
$\mathrm{n}_{\mathrm{t}}=$ number of bars in tension
$\emptyset_{\mathrm{t}}=$ diameter of bars in tension (mm)
$\mathrm{A}_{\mathrm{sc}}=$ area of steel in compression $\left(\mathrm{mm}^{2}\right)$
$\mathrm{n}_{\mathrm{c}}=$ number of bars in compression
$\emptyset_{\mathrm{c}}=$ diameter of bars in compression (mm)
$\emptyset_{\tau}=$ diameter of stirrups (mm)
$\mathrm{n}_{\mathrm{sl}}=$ number of ties
$\mathrm{S}=$ spacing of stirrups $(\mathrm{mm} / \mathrm{cc})$
$\mathrm{D}_{\mathrm{x}}=$ breadth of column (mm)
$\mathrm{D}_{\mathrm{y}}=$ depth of column (mm)
$\mathrm{M}_{\mathrm{ux}}=$ moment in X direction ( kNm )
$\mathrm{M}_{\mathrm{uy}}=$ moment in Y direction (kNm)
$\mathrm{P}_{\mathrm{u}}=$ axial load on compression member $(\mathrm{kN})$

| Table 5.1: Design of beam |  |  |  |
| :--- | :--- | :--- | :--- |
|  | value | units |  |
| breadth of beam (b) | 300 | mm |  |
| depth of beam (D) | 400 | mm |  |
| characteristic compressive <br> concrete $\left(\mathbf{f}_{\mathbf{c k}}\right)$ | strength of | 25 | MPa |
| characteristic strength of steel(f( $\mathbf{f}_{\mathbf{y}}$ ) | 415 | MPa |  |
| effective depth (d) | 350 | mm |  |
| effective span(l) | 6000 | mm |  |
| factored moment $\left(\mathbf{M}_{\mathbf{u}}\right)$ | 215.2 | kNm |  |
| $\mathbf{M}_{\mathbf{u}, \text { lim }}$ | 127.62 | kNm |  |
| check for singly or double reinforced beam | Mu <br> $\mathrm{Mu}, \mathrm{lim}$ | Doubly reinforced |  |
| $\mathbf{x}_{\mathbf{u}, \text { max }} / \mathbf{d}$ | 0.48 |  |  |
| $\mathbf{p}_{\mathbf{t}, \mathrm{lim}}$ | 1.2 | $\%$ |  |


|  |  |  |  |
| :---: | :---: | :---: | :---: |
| Determining $\mathrm{A}_{\text {st }}$ |  |  |  |
| balanced section where $\mathrm{x}_{\mathrm{u}}=\mathrm{x}_{\mathrm{u}, \text { max }}$ |  |  |  |
| $\mathbf{A}_{\text {st,lim }}$ | 1260 | $\mathrm{mm}^{2}$ |  |
| diameter of bars for tension steel(Ø) | 20 | mm |  |
| diameter of stirrups $\left(\emptyset_{\tau}\right)$ | 6 | mm |  |
| clear cover provided to the reinforcement | 30 | mm |  |
| effective cover to reinforcement( $\mathrm{d}^{\prime}$ ) | 46 | mm |  |
| $\left(\Delta \mathbf{A}_{\text {st }}\right)_{\text {reqd }}$ | 798 | $\mathrm{mm}^{2}$ |  |
| $\left(\mathbf{A s t}_{\text {st }}\right.$ reqd $^{\text {d }}$ | 2058 | $\mathrm{mm}^{2}$ |  |
| number of bars | 3 |  |  |
| $\emptyset_{\text {reqd }}$ | 30 | mm |  |
| $\mathbf{A}_{\text {st }}$ | 2121 | $\mathrm{mm}^{2}$ |  |
| actual d | 349 | mm |  |
| as actual $d$ is less than the $d$ assumed earlier so revising the above calculations by $\mathrm{d}=349 \mathrm{~mm}$ |  |  |  |
| $\mathbf{M}_{\mathrm{u}, \mathrm{lim}}$ | 126.89 | kNm |  |
| $\mathbf{A}_{\text {st,lim }}$ | 1256.4 | $\mathrm{mm}^{2}$ |  |
| $\left(\Delta \mathbf{A}_{\text {st }}\right)_{\text {reqd }}$ | 801 | $\mathrm{mm}^{2}$ |  |
| $\left(\mathbf{A}_{\text {st }}\right)_{\text {reqd }}$ | 2057.4 | $\mathrm{mm}^{2}$ |  |
| Actual ( $\left.\Delta \mathbf{A}_{\text {st }}\right)_{\text {provided }}$ | 864.6 | $\mathrm{mm}^{2}$ |  |
| Determining $\mathbf{A}_{\text {sc }}$ |  |  |  |
| assuming $\mathrm{x}_{\mathrm{u}}=\mathrm{x}_{\mathrm{u}, \text { max }}$ |  |  |  |
| d'/d | 0.132 |  |  |
| from table A |  |  |  |
| $\mathrm{f}_{\text {sc }}$ | 345.82 | MPa |  |
| ( $\left.\mathbf{A s c}_{\text {sc }}\right)_{\text {reqd }}$ | 933 | $\mathrm{mm}^{2}$ |  |
| number of bars | 5 |  |  |
| $\emptyset_{\text {reqd }}$ | 16 | mm |  |
| $\mathbf{A}_{\text {sc }}$ | 1006 | $\mathrm{mm}^{2}$ |  |
| Design Check |  |  |  |
| assuming $\mathrm{x}_{\mathrm{u}} \leq \mathrm{x}_{\mathrm{u}, \text { max }}$, it suffices to establish $\mathbf{p}_{\mathrm{c}} \geq$ $\mathbf{p}_{\mathrm{c}}{ }^{*}$ |  |  |  |
| actual d provided | 349 | mm |  |
| d' | 44 | mm |  |
| d'/d | 0.127 |  |  |
| from table A |  |  |  |
| $\mathrm{f}_{\text {sc }}$ | 346.77 | MPa |  |
| actual $\mathbf{p}_{\mathrm{t}}$ | 2.026 | \% |  |
| actual $\mathbf{p}_{\mathbf{c}}$ | 0.961 | \% |  |
| 38 |  |  |  |


| $\mathbf{p}_{\text {c }}{ }^{*}$ | 0.889 | \% |  |
| :---: | :---: | :---: | :---: |
| as $p_{c}>p_{c}{ }^{*}$, Hence OK |  |  |  |
| Check for deflection control |  |  |  |
| $\mathrm{p}_{\mathrm{t}}$ | 2.026 | \% |  |
| $\mathrm{f}_{\text {s }}$ | 234 | MPa |  |
| $\mathrm{k}_{\mathrm{t}}$ (from fig. 4 of code IS 456:2000) | 0.8468 |  |  |
| $\mathbf{p}_{\text {c }}$ | 0.961 | \% |  |
| $\mathbf{k}_{\mathrm{c}}$ (from fig. 5 of code IS 456:2000) | 1.2 |  |  |
| (l/d) max | 20.33 |  |  |
| (l/d) provided | 17.2 |  |  |
| as $(\mathbf{l} / \mathbf{d})_{\max }>(\mathbf{l} / \mathrm{d})_{\text {provided }}$, Hence OK |  |  |  |
|  |  |  |  |
| Shear Design |  |  |  |
|  |  |  |  |
| max. shear stress ( $\tau_{\text {cmax }}$ ) | 3.1 | MPa |  |
| factored shear force ( $\mathrm{V}_{\mathrm{u}}$ ) | 230.37 | kN |  |
| nominal shear stress ( $\tau_{\mathrm{v}}$ ) | 2.21 | MPa |  |
| $\beta$ | 1.44 |  |  |
| design shear strength of concrete ( $\tau_{c}$ ) | 0.82 | MPa |  |
| check whether $\tau_{\text {c,max }}>\tau_{c}$ | Yes |  |  |
| shear force resisted by concrete ( $\mathrm{V}_{\mathbf{u c}}$ ) | 85.86 | kN |  |
| check whether $\mathrm{V}_{\mathbf{u}}>\mathrm{V}_{\mathbf{u c}}$ | Yes | Provide rft.' |  |
| diameter of stirrups $\left(\emptyset_{\tau}\right)$ | 6 | mm |  |
| number of stirrup legs | 2 |  |  |
|  |  |  |  |
| Minimum shear reinforcement |  |  |  |
| stirrup spacing along beam length | 171 | $\mathrm{mm} / \mathrm{cc}$ |  |
| check whether stirrup spacing $<300 \mathrm{~mm}$ | Yes |  |  |
| provide stirrups of diameter | 6 mm | 2 legged | $\begin{array}{ll} 171 & \mathrm{~mm} \\ \mathrm{c} / \mathrm{c} \end{array}$ |
|  |  |  |  |
| Calculated shear reinforcement |  |  |  |
| shear force taken up by stirrups ( $\mathrm{V}_{\mathrm{us}}$ ) | 144.51 | kN |  |
| stirrup spacing along beam length | 50 | $\mathrm{mm} / \mathrm{cc}$ |  |
| check whether stirrup spacing < 300mm | Yes |  |  |
| provide stirrups of diameter | 6 mm | 2 legged | $\begin{array}{ll} \hline 50 & \mathrm{~mm} \\ \mathrm{c} / \mathrm{c} \end{array}$ |

### 5.3 Design of beams of building

### 5.3.1

Table 5.2: Beams in transverse direction

| Beam No. | $\begin{aligned} & \mathrm{bxD} \\ & \mathrm{~mm} \end{aligned}$ | d mm | $\begin{aligned} & \mathbf{M}_{\mathbf{u}} \\ & \mathbf{k N m} \end{aligned}$ | $\begin{aligned} & \mathbf{M}_{\mathrm{u}, \mathrm{lim}} \\ & \mathbf{k N m} \end{aligned}$ | $\begin{aligned} & \mathbf{A}_{\mathrm{st}} \\ & \mathbf{m m}^{2} \end{aligned}$ | $\mathbf{n}_{\text {t }}$ | $\begin{aligned} & \boldsymbol{\emptyset}_{\mathrm{t}} \\ & \mathbf{m m} \end{aligned}$ | $\begin{aligned} & \mathbf{A}_{\mathrm{sc}} \\ & \mathbf{m m}^{2} \end{aligned}$ | $\mathbf{n}_{\mathbf{c}}$ | $\begin{aligned} & \boldsymbol{\emptyset}_{\mathbf{c}} \\ & \mathrm{mm} \end{aligned}$ | Shear reinforcement |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  |  |  | $\begin{aligned} & \boldsymbol{\emptyset}_{\tau} \\ & \mathbf{m m} \end{aligned}$ | $\mathbf{n}_{\text {sl }}$ | $\begin{array}{\|l\|} \hline \mathbf{S} \\ \mathrm{mm} / \\ \mathbf{c c} \end{array}$ |
| 1 | $\begin{aligned} & \hline 300 \times 4 \\ & 00 \\ & \hline \end{aligned}$ | 349 | 215.2 | 127.62 | 2121 | 3 | 30 | 1006 | 5 | 16 | 6 | 2 | 50 |
| 2 | $\begin{aligned} & \hline 300 \times 4 \\ & 00 \\ & \hline \end{aligned}$ | $\begin{aligned} & \hline 349 . \\ & 5 \end{aligned}$ | $\begin{array}{\|l} \hline 198.2 \\ 3 \end{array}$ | 127.62 | 1982 | 3 | 29 | 884 | 5 | 15 | 6 | 2 | 49 |
| 3 | $\begin{aligned} & 300 \times 4 \\ & 00 \\ & \hline \end{aligned}$ | 349 | $\begin{array}{\|l} \hline 208.3 \\ 3 \\ \hline \end{array}$ | 127.62 | 2121 | 3 | 30 | 1006 | 5 | 16 | 6 | 2 | 48 |
| 4 | $\begin{array}{\|l\|} \hline 300 \times 4 \\ 00 \end{array}$ | 349 | $\begin{aligned} & 207.7 \\ & 1 \end{aligned}$ | 127.62 | 2121 | 3 | 30 | 1006 | 5 | 16 | 6 | 2 | 48 |
| 5 | $\begin{aligned} & \hline 300 \times 4 \\ & 00 \\ & \hline \end{aligned}$ | $\begin{aligned} & \hline 349 . \\ & 5 \\ & \hline \end{aligned}$ | $\begin{array}{\|l} \hline 196.8 \\ 8 \\ \hline \end{array}$ | 127.62 | 1982 | 3 | 29 | 884 | 5 | 15 | 6 | 2 | 49 |
| 6 | $\begin{aligned} & 300 \times 4 \\ & 00 \\ & \hline \end{aligned}$ | 349 | 209.1 | 127.62 | 2121 | 3 | 30 | 1006 | 5 | 16 | 6 | 2 | 48 |
| 7 | $\begin{aligned} & \hline 300 \times 4 \\ & 00 \end{aligned}$ | $\begin{aligned} & \hline 349 . \\ & 5 \end{aligned}$ | 192.8 | 127.62 | 1982 | 3 | 29 | 884 | 5 | 15 | 6 | 2 | 50 |
| 8 | $\begin{aligned} & 300 \times 4 \\ & 00 \\ & \hline \end{aligned}$ | 350 | $\begin{array}{\|l\|l\|} \hline 184.4 \\ \hline \end{array}$ | 127.62 | 1848 | 3 | 28 | 664 | 5 | 13 | 6 | 2 | 50 |
| 21 | $\begin{aligned} & 300 \times 4 \\ & 00 \\ & \hline \end{aligned}$ | 349 | $\begin{array}{\|l} 217.8 \\ 7 \\ \hline \end{array}$ | 127.62 | 2121 | 3 | 30 | 1006 | 5 | 16 | 6 | 2 | 45 |
| 22 | $\begin{aligned} & \hline 300 \times 4 \\ & 00 \end{aligned}$ | $\begin{array}{\|l} \hline 349 . \\ 5 \end{array}$ | $\begin{array}{\|l} \hline 201.9 \\ 9 \end{array}$ | 127.62 | 1982 | 3 | 29 | 884 | 5 | 15 | 6 | 2 | 47 |
| 23 | $\begin{aligned} & \hline 300 \times 4 \\ & 00 \\ & \hline \end{aligned}$ | 349 | $\begin{aligned} & \hline 210.6 \\ & 8 \end{aligned}$ | 127.62 | 2121 | 3 | 30 | 1006 | 5 | 16 | 6 | 2 | 46 |
| 24 | $\begin{aligned} & \hline 300 \times 4 \\ & 00 \\ & \hline \end{aligned}$ | 349 | $\begin{aligned} & \hline 212.1 \\ & 8 \end{aligned}$ | 127.62 | 2121 | 3 | 30 | 1006 | 5 | 16 | 6 | 2 | 46 |
| 25 | $\begin{array}{\|l\|} \hline 300 \times 4 \\ 00 \\ \hline \end{array}$ | $\begin{aligned} & \hline 349 . \\ & 5 \end{aligned}$ | $\begin{aligned} & 199.9 \\ & 6 \end{aligned}$ | 127.62 | 1982 | 3 | 29 | 884 | 5 | 15 | 6 | 2 | 47 |
| 26 | $\begin{aligned} & \hline 300 \times 4 \\ & 00 \end{aligned}$ | 349 | $\begin{array}{\|l} \hline 213.9 \\ 4 \end{array}$ | 127.62 | 2121 | 3 | 30 | 1006 | 5 | 16 | 6 | 2 | 46 |
| 27 | $\begin{aligned} & \hline 300 \times 4 \\ & 00 \\ & \hline \end{aligned}$ | 350 | $\begin{aligned} & 189.0 \\ & 3 \\ & \hline \end{aligned}$ | 127.62 | 1848 | 3 | 28 | 664 | 5 | 13 | 6 | 2 | 50 |
| 28 | $\begin{aligned} & \hline 300 \times 4 \\ & 00 \end{aligned}$ | 350 | $\begin{array}{\|l\|} \hline 182.2 \\ 6 \end{array}$ | 127.62 | 1848 | 3 | 28 | 664 | 5 | 13 | 6 | 2 | 51 |
| 41 | $\begin{aligned} & 300 \times 4 \\ & 00 \end{aligned}$ | 349 | 215.2 | 127.62 | 2121 | 3 | 30 | 1006 | 5 | 16 | 6 | 2 | 47 |
| 42 | $\begin{aligned} & \hline 300 \times 4 \\ & 00 \end{aligned}$ | $\begin{array}{\|l} \hline 349 . \\ 5 \end{array}$ | $\begin{aligned} & 198.2 \\ & 3 \end{aligned}$ | 127.62 | 1982 | 3 | 29 | 884 | 5 | 15 | 6 | 2 | 49 |
| 43 | $\begin{aligned} & 300 \times 4 \\ & 00 \\ & \hline \end{aligned}$ | 349 | $\begin{array}{\|l\|} \hline 208.3 \\ 3 \end{array}$ | 127.62 | 2121 | 3 | 30 | 1006 | 5 | 16 | 6 | 2 | 48 |


| 44 | $300 \times 4$ <br> 00 | 349 | 207.7 <br> 1 | 127.62 | 2121 | 3 | 30 | 1006 | 5 | 16 | 6 | 2 | 48 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 45 | $300 \times 4$ <br> 00 | 349. <br> 5 | 196.8 <br> 8 | 127.62 | 1982 | 3 | 29 | 884 | 5 | 15 | 6 | 2 | 49 |
| 46 | $300 \times 4$ <br> 00 | 349 | 209.1 | 127.62 | 2121 | 3 | 30 | 1006 | 5 | 16 | 6 | 2 | 48 |
| 47 | $300 \times 4$ <br> 00 | 349. <br> 5 | 192.8 | 127.62 | 1982 | 3 | 29 | 884 | 5 | 15 | 6 | 2 | 50 |
| 48 | $300 \times 4$ <br> 00 | 350 | 184.4 <br> 3 | 127.62 | 1848 | 3 | 28 | 664 | 5 | 13 | 6 | 2 | 50 |

### 5.3.2

Table 5.3: Beams in longitudinal direction

| Beam No. | $\begin{aligned} & \hline \text { bxD } \\ & \mathrm{mm} \end{aligned}$ | $\begin{aligned} & \mathrm{d} \\ & \mathrm{~mm} \end{aligned}$ | $\mathbf{M}_{\mathbf{u}}$ <br> kNm | $\begin{aligned} & \mathbf{M}_{\mathrm{u}, \mathrm{lim}} \\ & \mathbf{k N m} \end{aligned}$ | $\begin{aligned} & \mathbf{A}_{\mathrm{st}} \\ & \mathbf{m m}^{2} \end{aligned}$ | $\mathbf{n}_{\mathbf{t}}$ | $\begin{aligned} & \boldsymbol{\emptyset}_{\mathrm{t}} \\ & \mathbf{m m} \end{aligned}$ | $\begin{aligned} & \mathbf{A}_{\mathbf{s c}} \\ & \mathbf{m m}^{2} \end{aligned}$ | $\mathbf{n}_{\mathbf{c}}$ | $\begin{aligned} & \hline \emptyset_{\mathbf{c}} \\ & \mathrm{mm} \end{aligned}$ | Shear reinforcement |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  |  |  | $\begin{aligned} & \emptyset_{\tau} \\ & \mathrm{mm} \end{aligned}$ | $\mathbf{n}_{\text {sl }}$ | $\begin{aligned} & \mathrm{S} \\ & \mathrm{~mm} / \\ & \mathrm{cc} \end{aligned}$ |
| 61 | $\begin{aligned} & 300 \times 4 \\ & 50 \\ & \hline \end{aligned}$ | 399 | $\begin{aligned} & 252.3 \\ & 3 \\ & \hline \end{aligned}$ | 166.68 | 2121 | 3 | 30 | 764 | 3 | 18 | 6 | 2 | 56 |
| 62 | $\begin{aligned} & 300 \times 4 \\ & 50 \\ & \hline \end{aligned}$ | 399 | $\begin{aligned} & 242.7 \\ & 3 \\ & \hline \end{aligned}$ | 166.68 | 2121 | 3 | 30 | 764 | 3 | 18 | 6 | 2 | 57 |
| 63 | $\begin{aligned} & 300 \times 4 \\ & 50 \\ & \hline \end{aligned}$ | 399 | $\begin{aligned} & 252.3 \\ & 3 \end{aligned}$ | 166.68 | 2121 | 3 | 30 | 764 | 3 | 18 | 6 | 2 | 56 |
| 64 | $\begin{aligned} & 300 \times 4 \\ & 50 \end{aligned}$ | $\begin{array}{\|l} \hline 399 . \\ 5 \end{array}$ | $\begin{aligned} & 233.6 \\ & 4 \end{aligned}$ | 166.68 | 1982 | 3 | 29 | 604 | 3 | 16 | 6 | 2 | 59 |
| 65 | $\begin{aligned} & 300 \times 4 \\ & 50 \end{aligned}$ | $\begin{aligned} & \hline 399 . \\ & 5 \end{aligned}$ | $\begin{aligned} & 222.7 \\ & 8 \end{aligned}$ | 166.68 | 1982 | 3 | 29 | 604 | 3 | 16 | 6 | 2 | 60 |
| 66 | $\begin{aligned} & \hline 300 \times 4 \\ & 50 \end{aligned}$ | $\begin{array}{\|l} \hline 399 . \\ 5 \end{array}$ | $\begin{aligned} & 233.6 \\ & 4 \end{aligned}$ | 166.68 | 1982 | 3 | 29 | 604 | 3 | 16 | 6 | 2 | 59 |
| 67 | $\begin{aligned} & 300 \times 4 \\ & 50 \\ & \hline \end{aligned}$ | $\begin{array}{\|l} \hline 399 . \\ \hline \end{array}$ | $\begin{aligned} & 223.6 \\ & 05 \end{aligned}$ | 166.68 | 1982 | 3 | 29 | 604 | 3 | 16 | 6 | 2 | 63 |
| 68 | $\begin{aligned} & 300 \times 4 \\ & 50 \\ & \hline \end{aligned}$ | $\begin{array}{\|l} \hline 399 . \\ \hline 5 \\ \hline \end{array}$ | $\begin{aligned} & \hline 228.3 \\ & 6 \\ & \hline \end{aligned}$ | 166.68 | 1982 | 3 | 29 | 604 | 3 | 16 | 6 | 2 | 61 |
| 69 | $\begin{aligned} & 300 \times 4 \\ & 50 \end{aligned}$ | $\begin{aligned} & 399 . \\ & 5 \end{aligned}$ | $\begin{aligned} & 221.8 \\ & 5 \end{aligned}$ | 166.68 | 1982 | 3 | 29 | 604 | 3 | 16 | 6 | 2 | 63 |
| 70 | $\begin{aligned} & 300 \times 4 \\ & 50 \end{aligned}$ | 400 | $\begin{aligned} & \hline 205.3 \\ & 35 \\ & \hline \end{aligned}$ | 166.68 | 1848 | 3 | 28 | 462 | 3 | 14 | 6 | 2 | 65 |
| 71 | $\begin{aligned} & 300 \times 4 \\ & 50 \\ & \hline \end{aligned}$ | 400 | $\begin{aligned} & 205.1 \\ & 4 \\ & \hline \end{aligned}$ | 166.68 | 1848 | 3 | 28 | 462 | 3 | 14 | 6 | 2 | 65 |
| 72 | $\begin{aligned} & 300 \times 4 \\ & 50 \\ & \hline \end{aligned}$ | 400 | $\begin{aligned} & 204.3 \\ & 3 \end{aligned}$ | 166.68 | 1848 | 3 | 28 | 462 | 3 | 14 | 6 | 2 | 65 |
| 73 | $\begin{array}{\|l\|} \hline 300 \times 4 \\ 50 \\ \hline \end{array}$ | $\begin{array}{\|l} \hline 398 . \\ 5 \\ \hline \end{array}$ | $\begin{aligned} & 264.1 \\ & 05 \\ & \hline \end{aligned}$ | 166.68 | 2265 | 3 | 31 | 943 | 3 | 20 | 6 | 2 | 58 |
| 74 | $\begin{aligned} & 300 \times 4 \\ & 50 \\ & \hline \end{aligned}$ | $\begin{array}{\|l\|} \hline 398 . \\ 5 \\ \hline \end{array}$ | $\begin{aligned} & \hline 255.3 \\ & 45 \\ & \hline \end{aligned}$ | 166.68 | 2265 | 3 | 31 | 943 | 3 | 20 | 6 | 2 | 59 |
| 41 |  |  |  |  |  |  |  |  |  |  |  |  |  |


| 75 | $300 \times 4$ <br> 50 | 398. <br> 5 | 264.1 <br> 05 | 166.68 | 2265 | 3 | 31 | 943 | 3 | 20 | 6 | 2 | 58 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 76 | $300 \times 4$ <br> 50 | 398. <br> 5 | 270.6 <br> 9 | 166.68 | 2265 | 3 | 31 | 943 | 3 | 20 | 6 | 2 | 56 |
| 77 | $300 \times 4$ <br> 50 | 398. <br> 5 | 265.1 <br> 4 | 166.68 | 2265 | 3 | 31 | 943 | 3 | 20 | 6 | 2 | 56 |
| 78 | $300 \times 4$ <br> 50 | 398. <br> 5 | 270.6 <br> 9 | 166.68 | 2265 | 3 | 31 | 943 | 3 | 20 | 6 | 2 | 56 |
| 79 | $300 \times 4$ <br> 50 | 398. <br> 5 | 263.2 <br> 2 | 166.68 | 2265 | 3 | 31 | 943 | 3 | 20 | 6 | 2 | 56 |
| 80 | $300 \times 4$ <br> 50 | 398. <br> 5 | 261.7 <br> 65 | 166.68 | 2265 | 3 | 31 | 943 | 3 | 20 | 6 | 2 | 56 |
| 81 | $300 \times 4$ <br> 50 | 398. <br> 5 | 263.2 <br> 2 | 166.68 | 2265 | 3 | 31 | 943 | 3 | 20 | 6 | 2 | 56 |
| 82 | $300 \times 4$ <br> 50 | 399. <br> 5 | 221.7 <br> 75 | 166.68 | 1982 | 3 | 29 | 604 | 3 | 16 | 6 | 2 | 63 |
| 83 | $300 \times 4$ <br> 50 | 399. <br> 5 | 218.7 <br> 75 | 166.68 | 1982 | 3 | 29 | 604 | 3 | 16 | 6 | 2 | 63 |
| 84 | $300 \times 4$ <br> 50 | 399. <br> 5 | 221.7 <br> 5 | 166.68 | 1982 | 3 | 29 | 604 | 3 | 16 | 6 | 2 | 63 |

### 5.4 Design of columns

A compression member is a structural element which is subjected to axial compressive forces. Compression members are most commonly encountered in reinforced concrete buildings as columns forming part of vertical framing system. Whether the structure is man made or created by nature the key element in resisting collapse under gravity load is the column. The column is representative of all types of compression members and hence sometimes the terms column and compression member are used interchangeably.

### 5.5 Spreadsheet of design of short columns under axial compression with biaxial bending

Table 5.4 Design of Column

|  | values | units |
| :--- | :--- | :--- |
| breadth of column $(\mathbf{b})\left(\mathbf{D}_{\mathbf{x}}\right)$ | 300 | mm |
| depth of column $(\mathbf{D})\left(\mathbf{D}_{\mathbf{y}}\right)$ | 500 | mm |
| unsupported length of column (I) | 3500 | mm |
| $\mathbf{P}_{\mathbf{u}}$ | 1461.79 | kN |
| $\mathbf{M}_{\mathrm{ux}}$ | 65.72 | kNm |
| $\mathbf{M}_{\mathbf{u y}}$ | 27.71 | kNm |
| characteristic strength of steel $\left(\mathbf{f}_{\mathbf{y}}\right)$ | 415 | MPa |
| characteristic <br> concrete $\left(\mathbf{f}_{\mathrm{c}}\right)$ | compressive strength $\quad$ of | 25 |
| Slenderness ratio | MPa |  |


|  |  |  |
| :---: | :---: | :---: |
| effective length ratio | 0.85 |  |
| effective length about $x$-x axis ( $\mathrm{l}_{\mathrm{ex}}$ ) | 2975 | mm |
| effective length about $\mathbf{y}$ - y axis ( $\left(\mathrm{l}_{\mathrm{e}}\right)$ | 2975 | mm |
| $\mathrm{l}_{\text {ex }} / \mathrm{D}_{\mathrm{x}}$ | 9.92 |  |
| $\mathrm{l}_{\mathrm{ey}} / \mathrm{D}_{\mathrm{y}}$ | 5.95 |  |
| check for $\mathrm{l}_{\mathrm{ey}} / \mathrm{D}_{\mathrm{y}}$ | Yes short column |  |
| check for $\mathrm{l}_{\mathrm{ex}} / \mathrm{D}_{\mathrm{x}}$ | Yes short column |  |
| Check minimum eccentricities |  |  |
| Applied eccentricities |  |  |
| $\mathrm{e}_{\mathrm{x}}$ | 44.96 | mm |
| $\mathbf{e}_{\mathrm{y}}$ | 18.96 | mm |
| Minimum eccentricities |  |  |
| $\mathbf{e x}_{\mathrm{x}, \text { min }}$ | 20 | mm |
| $\mathbf{e x}_{\mathrm{y}, \mathrm{min}}$ | 23.67 | mm |
| Longitudinal reinforcement |  |  |
| $\mathrm{M}_{\mathrm{u}}$ | 83 | kNm |
| depth of compression reinforcement (d') | 50 | mm |
| d'/D | 0.1 |  |
| $\mathrm{p}_{\mathbf{u}}$ | 0.39 |  |
| $\mathrm{m}_{\mathbf{u}}$ | 0.03 |  |
| from chart 44 of SP16, $\mathrm{p} / \mathrm{f}_{\text {ck }}$ | 0.02 |  |
| $\mathrm{p}_{\text {reqd }}$ | 0.5 |  |
| $\mathbf{A}_{\text {s,reqd }}$ | 750 | $\mathrm{mm}^{2}$ |
| number of bars | 6 |  |
| $\emptyset$ | 18 | mm |
| $\mathbf{A}_{\text {s }}$ | 1527 | $\mathrm{mm}^{2}$ |
| provide 6 bars of 18mm dia |  |  |
| $\mathbf{p}_{\text {provided }}$ | 1.02 | \% |
| $\mathrm{p} / \mathrm{f}_{\text {ck }}$ | 0.05 |  |
|  |  |  |
| along $\mathrm{x}-\mathrm{x}$ axis |  |  |
| d'/D | 0.17 |  |
| from SP16 value of $\mathrm{m}_{\text {ux }}$ | 0.06 |  |
| $\mathrm{M}_{\mathrm{ux} 1}$ | 112.5 | kNm |
|  |  |  |
| along y -y axis |  |  |
| d'/D | 0.1 |  |


| from SP16 value of $\mathbf{m}_{\mathbf{u y}}$ | 0.08 |  |
| :--- | :--- | :--- |
| $\mathbf{M}_{\mathbf{u y} 1}$ | 150 | kNm |
| $\mathbf{P}_{\mathbf{u z}}$ |  |  |
| $\mathbf{P}_{\mathbf{u}} / \mathbf{P}_{\mathrm{uz}}$ | 2145.6 | kN |
| $\boldsymbol{\alpha}_{\mathbf{n}}$ | 0.69 |  |
|  | 1.82 |  |
| check safety under biaxial loading |  | trial section is <br> safe |
|  | 0.43 |  |
| Transverse reinforcement |  |  |
| tie diameter $\left(\boldsymbol{\emptyset}_{\mathbf{t}}\right.$ ) | 6 | mm |
| tie spacing $\left(\mathbf{s}_{\mathbf{t}}\right)$ | 288 | mm |
| provide 6 $\boldsymbol{\emptyset}$ ties @ 288c/c |  |  |

### 5.6 Table 5.5: Design of columns of building

| Column No. | $\begin{aligned} & \mathbf{D}_{\mathbf{x}} \mathbf{x} \\ & \mathbf{D}_{\mathbf{y}} \\ & \mathbf{m m} \end{aligned}$ | $\begin{aligned} & \mathrm{l} \\ & \mathbf{m m} \end{aligned}$ | $\begin{aligned} & \mathbf{P}_{\mathbf{u}} \\ & \mathbf{k} \mathbf{N} \end{aligned}$ | $\begin{aligned} & \mathbf{M}_{\mathrm{ux}} \\ & \mathbf{k N m} \end{aligned}$ | $\begin{aligned} & \mathbf{M}_{\mathrm{uy}} \\ & \mathbf{k N m} \end{aligned}$ | $\begin{aligned} & \hline \mathbf{M}_{\mathbf{u}} \\ & \mathbf{k N m} \end{aligned}$ | Longitudinal reinforcement |  |  | Transverse reinforcement |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | $\begin{aligned} & \mathbf{A}_{\mathbf{s}} \\ & \mathbf{m m}^{2} \end{aligned}$ | $\begin{aligned} & \emptyset \\ & \mathbf{m} \\ & \mathbf{m} \end{aligned}$ | No.of bars | $\begin{array}{\|l\|l} \hline \boldsymbol{\emptyset}_{\mathrm{t}} \\ \mathbf{m m} \end{array}$ | $\begin{array}{\|l\|} \hline \mathbf{S} \\ \mathbf{m m} / \mathbf{c c} \end{array}$ |
| 9 | $\begin{array}{\|l\|} \hline 300 \\ \mathrm{x} \\ 500 \\ \hline \end{array}$ | 3500 | 1461.79 | 65.72 | 27.71 | 83 | 1527 | 18 | 6 | 6 | 288 |
| 10 | $\begin{array}{\|l\|} \hline 300 \\ \mathrm{x} \\ 500 \\ \hline \end{array}$ | 3500 | 2528.01 | 47.53 | 28.18 | 64 | 3927 | 25 | 8 | 8 | 300 |
| 11 | $\begin{aligned} & \hline 300 \\ & \mathrm{x} \\ & 500 \\ & \hline \end{aligned}$ | 3500 | 1551.8 | 83.82 | 27.71 | 102 | 1527 | 18 | 6 | 6 | 288 |
| 12 | $\begin{array}{\|l\|} \hline 300 \\ \mathrm{x} \\ 500 \\ \hline \end{array}$ | 3500 | 1109.05 | 93.2 | 19.04 | 110 | 1527 | 18 | 6 | 6 | 288 |
| 13 | $\begin{array}{\|l\|} \hline 300 \\ \mathrm{x} \\ 500 \\ \hline \end{array}$ | 3500 | 1897.6 | 42.51 | 21.57 | 55 | 1885 | 20 | 6 | 6 | 300 |
| 14 | $\begin{aligned} & \hline 300 \\ & \mathrm{x} \\ & 500 \end{aligned}$ | 3500 | 1171.93 | 120.4 | 21.74 | 141 | 1527 | 18 | 6 | 6 | 288 |
| 15 | $\begin{array}{\|l} \hline 300 \\ \mathrm{x} \\ 500 \\ \hline \end{array}$ | 3500 | 741.4 | 85.38 | 22.19 | 102 | 1527 | 18 | 6 | 6 | 288 |

$\left.\begin{array}{|l|l|l|l|l|l|l|l|l|l|l|l||}\hline 16 & \begin{array}{l}300 \\ \mathrm{x} \\ 500\end{array} & 3500 & 1263.47 & 37.21 & 24.27 & 52 & 1527 & 18 & 6 & 6 & 288 \\ \hline 17 & \begin{array}{l}300 \\ \mathrm{x} \\ 500\end{array} & 3500 & 775.48 & 107.21 & 24.69 & 127 & 1527 & 18 & 6 & 6 & 288 \\ \hline 18 & \begin{array}{l}300 \\ \mathrm{x} \\ 500\end{array} & 3500 & 359.68 & 148.25 & 29.22 & 174 & 1527 & 18 & 6 & 6 & 288 \\ \hline 19 & \begin{array}{l}300 \\ \mathrm{x} \\ 500\end{array} & 3500 & 628.44 & 27.07 & 32.12 & 49 & 1527 & 18 & 6 & 6 & 288 \\ \hline 20 & \begin{array}{l}300 \\ \mathrm{x} \\ 500\end{array} & 3500 & 371.26 & 165.48 & 31.42 & 194 & 1527 & 18 & 6 & 6 & 288 \\ \hline 300 & 3500 & 1960.17 & 68.91 & 37.76 & 91 & 2946 & 25 & 6 & 6 & 300 \\ \hline & & & & & & & & & & & \\ 500\end{array}\right)$

| 49 | $\begin{aligned} & \hline \hline 300 \\ & \mathrm{x} \\ & 500 \end{aligned}$ | 3500 | 1610.4 | 57.34 | 39.36 | 80 | 1527 | 18 | 6 | 6 | 288 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 50 | $\begin{array}{\|l\|} \hline 300 \\ \mathrm{x} \\ 500 \\ \hline \end{array}$ | 3500 | 2641.98 | 47.53 | 41.02 | 73 | 7069 | 30 | 10 | 7.5 | 300 |
| 51 | $\begin{array}{\|l\|} \hline 300 \\ \mathrm{x} \\ 500 \end{array}$ | 3500 | 1610.4 | 83.82 | 39.36 | 107 | 1527 | 18 | 6 | 6 | 288 |
| 52 | $\begin{array}{\|l\|} \hline 300 \\ \mathrm{x} \\ 500 \\ \hline \end{array}$ | 3500 | 1208.6 | 101.21 | 47.18 | 129 | 1527 | 18 | 6 | 6 | 288 |
| 53 | $\begin{array}{\|l\|} \hline 300 \\ \mathrm{x} \\ 500 \\ \hline \end{array}$ | 3500 | 1972.25 | 42.51 | 50.69 | 77 | 2946 | 25 | 6 | 6.25 | 300 |
| 54 | $\begin{array}{\|l} \hline 300 \\ \mathrm{x} \\ 500 \\ \hline \end{array}$ | 3500 | 1208.6 | 120.4 | 47.18 | 149 | 1527 | 18 | 6 | 6 | 288 |
| 55 | $\begin{array}{\|l\|} \hline 300 \\ \mathrm{x} \\ 500 \\ \hline \end{array}$ | 3500 | 793.17 | 91.77 | 47.05 | 119 | 1527 | 18 | 6 | 6 | 288 |
| 56 | $\begin{array}{\|l\|} \hline 300 \\ \mathrm{x} \\ 500 \\ \hline \end{array}$ | 3500 | 1301.25 | 37.21 | 49.66 | 72 | 1527 | 18 | 6 | 6 | 288 |
| 57 | $\begin{array}{\|l\|} \hline 300 \\ \mathrm{x} \\ 500 \\ \hline \end{array}$ | 3500 | 793.17 | 107.21 | 47.05 | 135 | 1527 | 18 | 6 | 6 | 288 |
| 58 | $\begin{array}{\|l\|} \hline 300 \\ \mathrm{x} \\ 500 \\ \hline \end{array}$ | 3500 | 375.5 | 152.16 | 45.41 | 183 | 1527 | 18 | 6 | 6 | 288 |
| 59 | $\begin{array}{\|l\|} \hline 300 \\ \mathrm{x} \\ 500 \\ \hline \end{array}$ | 3500 | 639.19 | 27.07 | 48.13 | 64 | 1527 | 18 | 6 | 6 | 288 |
| 60 | $\begin{array}{\|l} \hline 300 \\ \mathrm{x} \\ 500 \\ \hline \end{array}$ | 3500 | 375.5 | 165.48 | 45.41 | 198 | 1527 | 18 | 6 | 6 | 288 |

## Conclusions

From the work presented above the following conclusions can be made :

1. From the Table 3.2 it was concluded that the value of forces that building can take are coming less in dynamic analysis as compared to static analysis. This shows that if design of building is done using dynamic analysis though we have to perform more calculations but it give more precise results as compared.
2. While carrying out response spectrum analysis consideration of infill wall in stiffness leads to better estimation of earthquake forces.
3. Software analysis and design using staad pro saves a lot of time spent in computation of results.
4. From the Table 4.1, Table 4.2, Table 4.3 and Table 4.4 it was concluded that response spectrum analysis is more economical.

In work presented above design, spread sheets for doubly reinforced beam and biaxial column were prepared. Their reinforcement detail is calculated from spread sheet and the results were tabulated.

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